

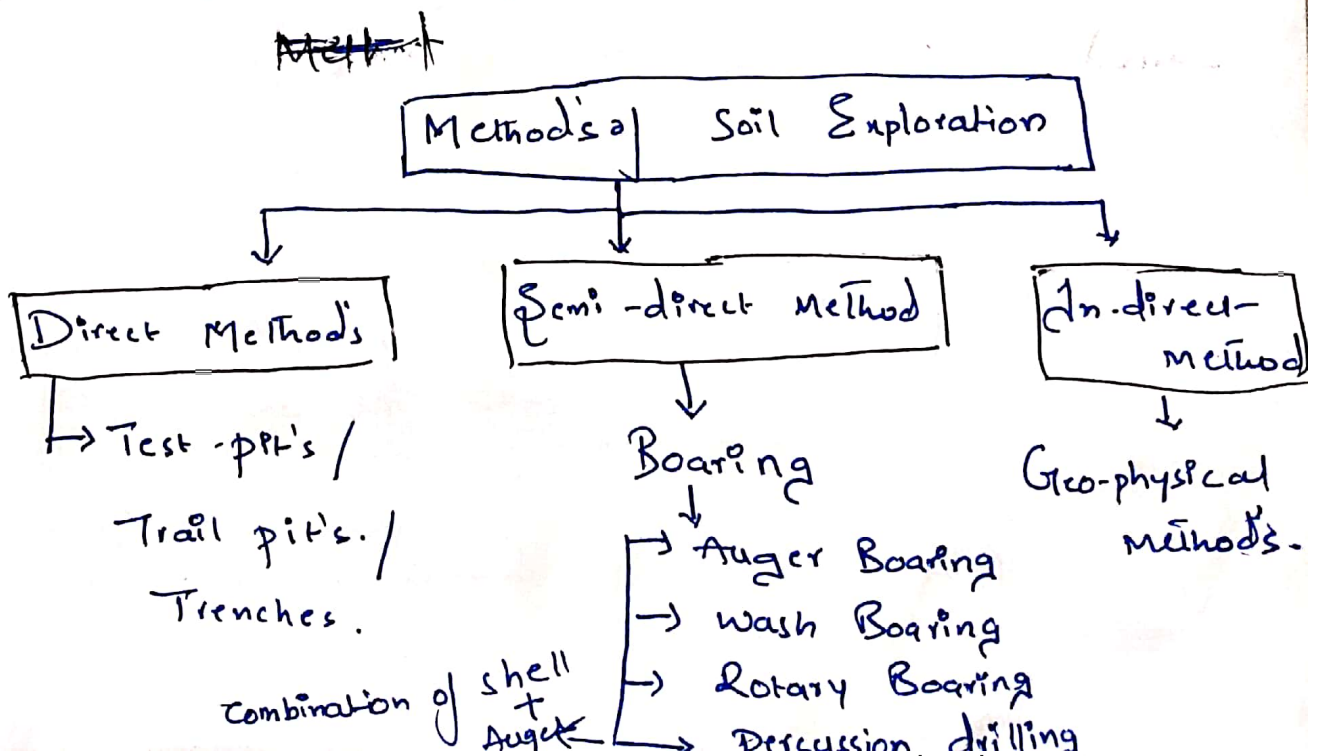
MODULE - I

Soil Exploration & Retaining walls:

Def: Soil Exploration consists of Determining the profile of the Natural soil deposit's @ site, taking the soil samples and Determining the Engg. Properties of soil using Laboratory tests as well as In-situ Testing Method's.

Need of Soil Exploration:-

- it gives the Information to determine the type of foundation required such as shallow or a deep foundation.
- Necessary Information with regard's to the strength & Compressibility characteristic's of the sub soil to allow the Design consultant to Make Recommendation's on the Safe Bearing pressure's or pile load Capacity.



Test-pit's :-

- It is the oldest method of soil exploration
- Test pit's give's the detailed visual examination of the sub-surface material in-situ condition.
- These are the open type.
- Disturbed or partially undisturbed samples can be obtained.
- Accessible in natural condition of soil.
- Suitable for smaller depths i.e. depths $\leq 3M$
- Cost increases with depth
- Greater depths may also need bracing lateral supports.
- Ground if encountered should be lowered.
- Suitable for small projects where the depth of foundation is ^{less} or shallow depths.

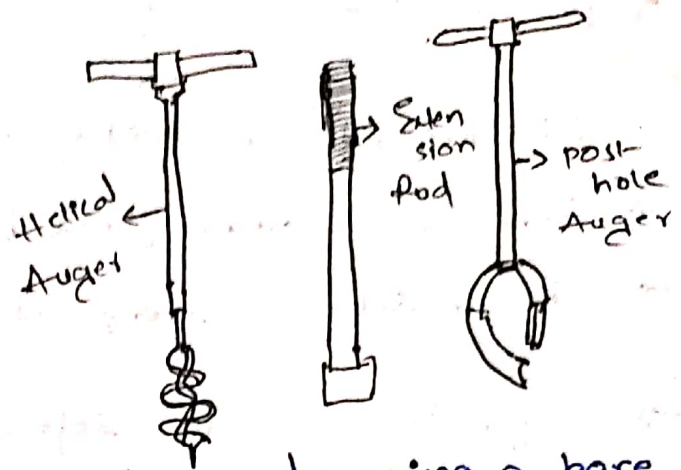
Boring Def:- Drilling bore hole's into ground to obtain soil / rock sample's from specified or unknown depths is called

Auger - Boring's

→ Auger's are of two types.

i) Hand operated Auger's

ii) Power Driven Auger's.



→ Auger's are the devices that are useful for advancing a bore hole into the ground.

→ Hand operated Auger's are used for relatively small depths, i.e. 3 to 5 m.

→ Power Driven Auger's are used for greater depths, i.e. up to 60 to 70 m [for continuous flight-augers].

→ Auger's are suitable for all types of soils which are presenting above w.T.

→ These are suitable only below w.T. in clayey soils.

Process

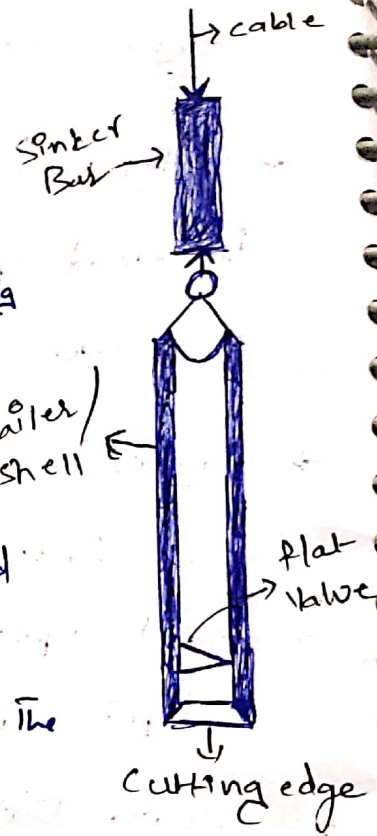
The soil Auger is advanced by rotating it while pressing it into the soil.

As soon as the Auger gets filled with soil, it is taken out and soil sample is collected.

The soil samples obtained from this type of borings are highly disturbed.

Auger & Shell Boring:

- This method was widely used in India.
- it is also known as sand bailer
- it consists of heavy duty pipe with cutting edge.
- Auger is used for soft clay soils & shell is used for stiff clay.
- Some times sinker bars are added to add weight to the bailer.
- Raising & Dropping of a shell in a hole cuts the soil
- Now soil is pushed in to tube/shell & emptied when full.
- Shell is used when auger boring becomes difficult



Wash Boring:

- it was commonly used for Boring in difficult soils.
- it was used when the exploration's are to be done below ~~the~~ WOT where auger is unsuitable.
- A casing pipe is pushed in & driven with a drop weight.
- Soil particles/sample is a very disturbed sample which was not suitable for evaluation of soil properties
- The change in color of water indicates the change of soil strata.

Process

A casing pipe is pushed in and driven with a drop weight.

hallow drill bit is screwed to a hallow drill rod connected to a rope passing over a pulley and supported by a tripod.

water jet under pressure is forced through the rod & the bit into the hole which loosens the soil.

The soil water suspension forced upward is led to a settling tank where the soil particles settle while the water over flows into a sump.

Rotary Drilling:

- it was normally used in rocky strata.
- it was very fast method & rock cores also obtained by suitable drill bits.

Process

A Drill bit, is fixed to the lower end of a drill rod & it is rotated by power

Drilling fluid / bentonite slurry is forced under pressure through the drill rod & it comes up bringing the cuttings to surface.

When the soil samples are read, the drill rod raised & drill bit is replaced by a sampler.

Percussion

Drilling

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Penetration Tests:-

(08) : Field Methods to Determine Bearing Capacity:-

i Here we have Mainly 3 type's of Tests.

i) plate Load Test

ii) Standard penetration Test

iii) Static cone penetration Test.

i) Plate- Load Test:-

→ These tests are used to determine The Bearing Capacity of soil's in An situ condition.

→ An plate - Load test we are taking a Steel plate of 30 cm or 45 cm or 60 cm or 90 cm.

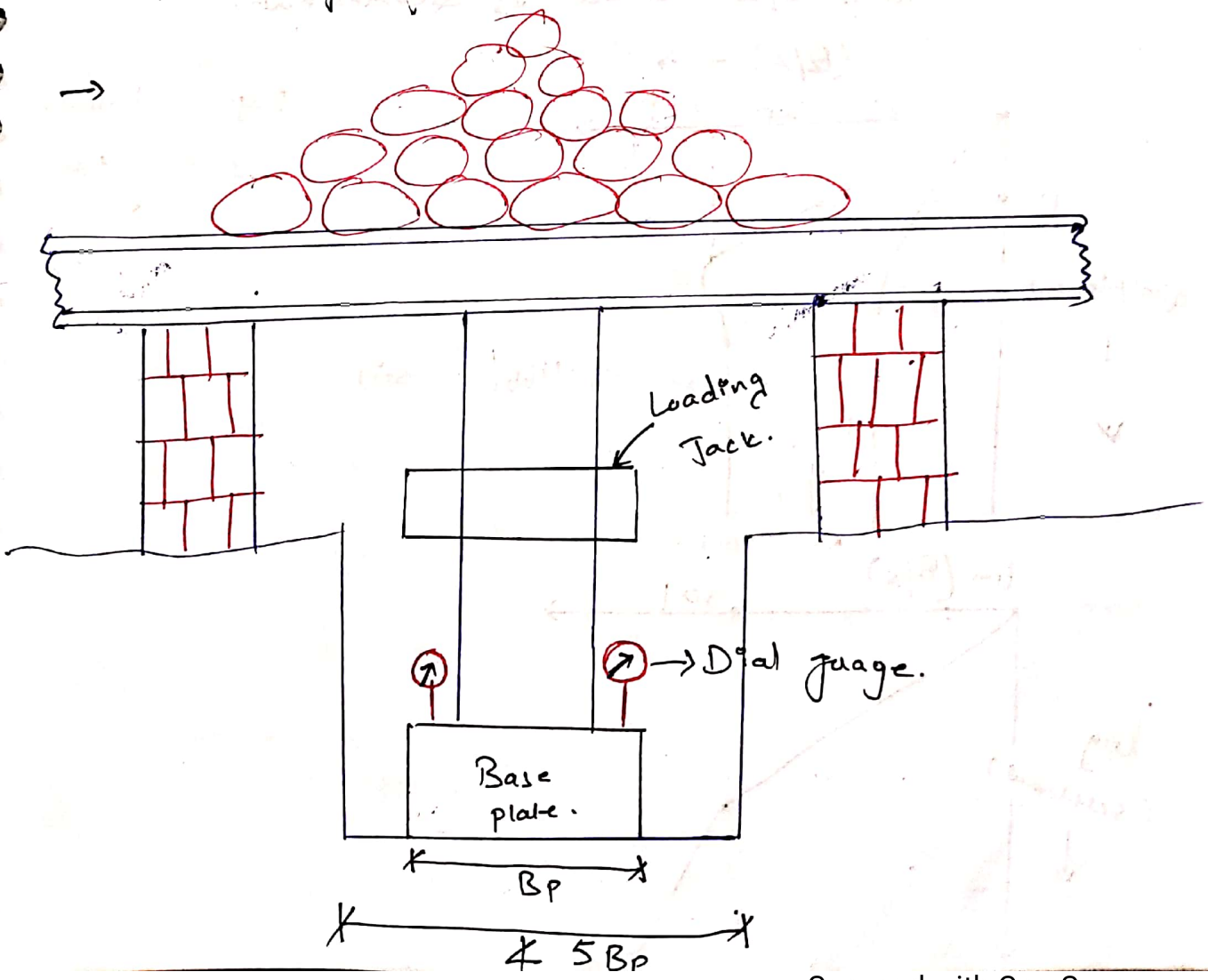
→ Shape of steel plate will depend's on shape of footing we design. Ex:- if we are going to design circular footing Take circular plate .Like wise rectangular or square ---

→ This plate [Baseplate] should be kept in a excavated Pit / trench.

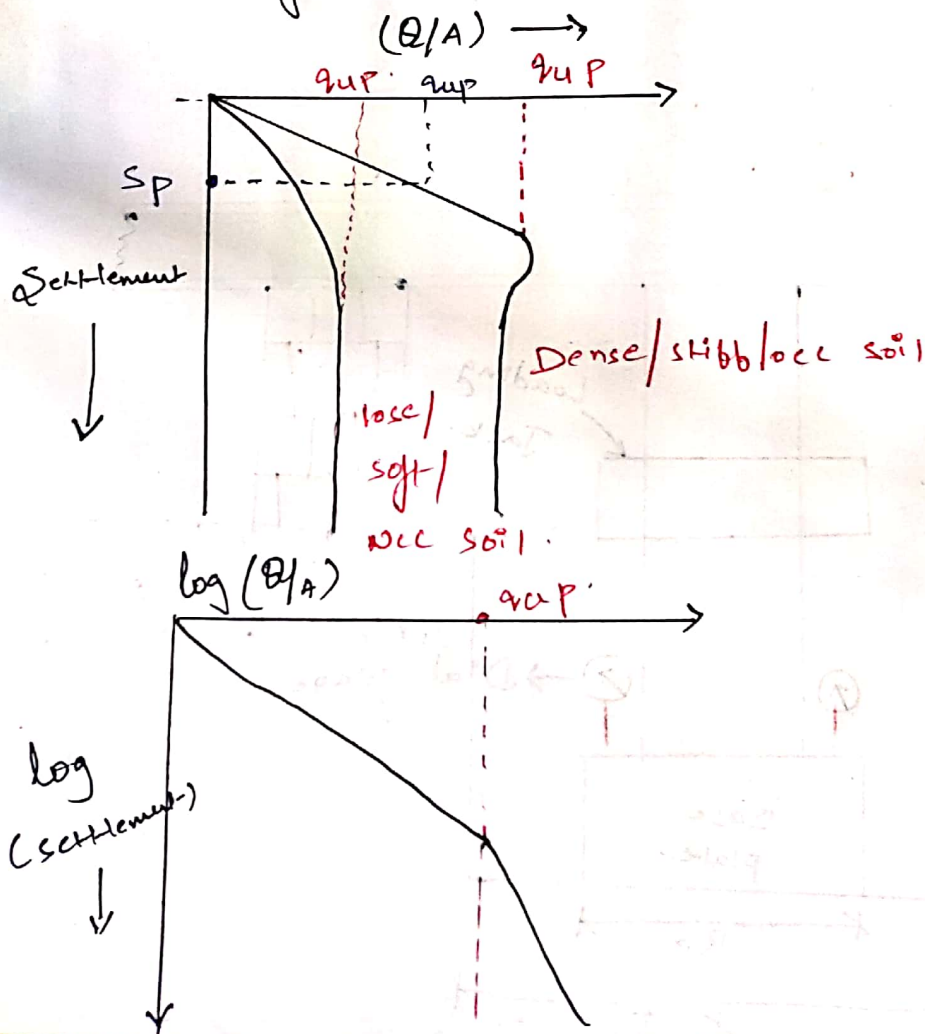
→ size of trench should be minimum of 150 cm. width

→ let B_p is width of Base plate.

- Now width of Trench $\neq 5 B_p$.
- Depth of Trench will be kept Equal to The Depth of footing which we have to be designed.
- on The base plate a loading Jack was arranged & 3 dial gauges are placed to note down The Settlement.
- 3 dial gauges are placed @ 120° from each other.
- we can use The single dial gauge to take Settlement readings but in case of Differential Settlement single Dial gauge reading will not gives accurate results.
- so we can arrange 3 dial gauges' reading & Take The average of 3 readings as Settlement.



- to start the test we need to apply the load on girder by manually or by using loading jack.
- when we started loading we can see the deflection's in dial gauge.
- as load ↑ dial gauge readings ↑.
- at certain point on ↑ of load we can see the large deflection in dial gauge
- it will indicate the soil below plate was suddenly settled i.e soil was failed @ that loading.
- we will stop loading at that point and we draw a graph b/w Load vs Settlement.



q_{up} = ultimate point of failure

lose / soft / occ soil
Dense / stiff / occ soil

→ for occ/stiff/ Dense soil q_{up} will be clear. but-
 in case of occ/lose/soft soil getting q_{up} is difficult because
 of the progressive settlement.

→ so to get q_{up} in occ/lose/soft soil we use log-log scale graph

Case (i) for clay soil:- In case of clay soil U.B.C does not
 depend upon the size of footing.

$$q_{uf} = q_{up} \quad \text{kN/m}^2 \quad \text{①}$$

q_{uf} = U.B.C of footing.

q_{up} = U.B.C of plate.

Case II :- in case of cohesion less/or sandy soil's

UBC depends on size of footing. i.e. ($q_{uf} \neq q_{up}$)

Assume in linear relationship

$$\frac{q_{uf}}{q_{up}} = \frac{B_f}{B_p}$$

$$q_{uf} = \frac{B_f \times q_{up}}{B_p} \quad \text{kN/m}^2 \quad \text{②}$$

B_f = width of footing

B_p = width of plate

Housel's Analysis:-

According to Housel the load carrying capacity
 is influenced by area and perimeter of the footing &
 properties of the soil.

→ if Q, A, P are ultimate load, Area of plate & perimeter of the plate respectively. Then as per Housel's.

$$Q = Am + Pn$$

Q = ultimate load
 A = Area of plate
 P = perimeter
 m, n = Properties of soil.

for 1st Base plate

$$Q_1 = A_1 m + P_1 n \rightarrow \textcircled{A}$$

for 2nd Base plate:

$$Q_2 = A_2 m + P_2 n \rightarrow \textcircled{B}$$

Here we have two eqn's & two unknowns if we solve both we get the values of m & n .

Now Assume A_f = Area of footing

P_f = perimeter of footing.

$$Q_f = A_f m + P_f n \quad \text{KN.}$$

U.B.C Based on Settlement Criteria:

Is code have suggested permissible values of settlement

for clay \Rightarrow 40 mm
for sand \Rightarrow 25 mm.

$$\frac{S_f}{S_p} = \left[\frac{B_f (B_p + 0.3)}{B_p (B_f + 0.3)} \right]^2 \quad (\text{for sandy soils.})$$

$$\frac{S_f}{S_p} = \left[\frac{B_f}{B_p} \right]^{n+1} \quad [\text{for } c-\phi \text{ soils here } n=0.5]$$

$$\frac{S_f}{S_p} = \left[\frac{B_f}{B_p} \right] \quad [\text{for clay soils}]$$

Here

S_f = Settlement of footing
 S_p = Settlement of plate.

in 'm' strictly. } B_f = width of footing (in m)
 B_p = width of plate (in m)

from this method

→ for the given permissible values of Settlement of footing (S_f), Settlement of plate (S_p) can be calculated.

→ Using load Settlement curve, ^{for the} values of S_p , q_{up} can be calculated.

→ Now using q_{up} ; q_{uf} can be calculated by using $S_{in} \text{ ① \& ②}$ for given soils.

Note:- No. further F.O.S is reqd because calculated value

of q_{up} has been estimated considering permissible Settlement of footings. q_{up} can be called safe/allowable pressure (in kN/m^2)

Limitations:-

i) The values of Bearing capacities we get from this test will show the ~~same~~ characteristics of small depth soil but in actual condition of footing's load distribution will be large.

it will show the maximum $\frac{1}{2}$ of width of plate width of soil characteristics will be shown.

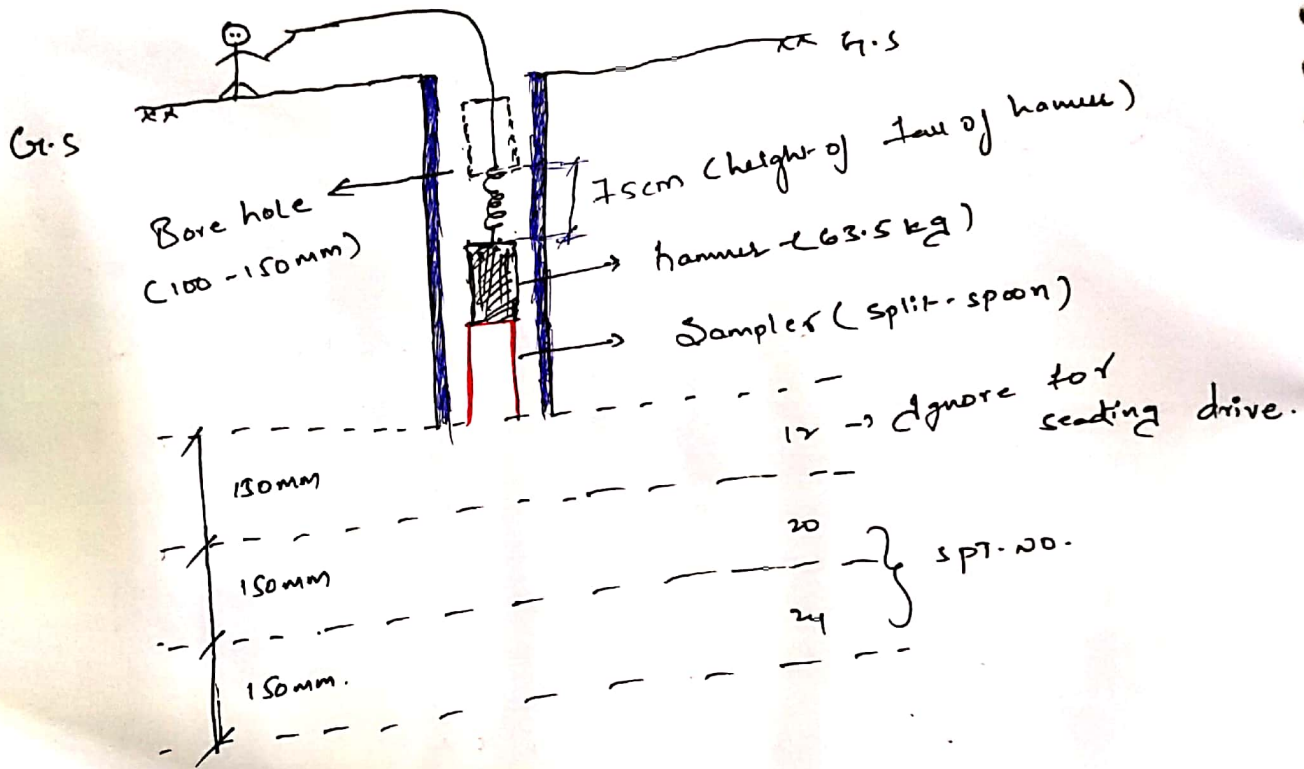
i.e. if we take 45 cm plate then it will show's maximum 90 cm depth characteristics.

ii) for clay soil's but is = 9 up.

but in clay's settlement takes a time (unseason)

But the test will be done in finite time.

Standard Penetration Test [spt. test] [Is 2131-1981]



- This test is performed in clean Bore hole of size 100 to 150mm
- Is 2131-1981 is used for this test.
- In bore hole's, casing and drilling mud can be used when drilling is to be done in soft clay or loose sand
- This test is ~~performed~~ performed @
 - i) at every change in strata
 - ii) @ Interval's not more than 1.5m } whichever is less.
- The sampler is penetrated at the bottom of the bore hole by dynamic mechanism of hammer

→ The weight of hammer & height of freefall are 63.5 kg and 75 cm respectively

→ The split-spoon sampler is first allowed to sink by its own self weight then no. of blows are applied.

→ This test is performed in 3 stages of 150 mm each.

→ The no. of blows used in first 150 mm penetration of sampler are ignored for seating drive.

→ The total no. of blows required in last 300 mm penetration of sampler is given as SPT value or SPT number.

→ Sometimes entire sampler sinks into the soil due to its self weight only. In that case no hammer blows are used SPT values can be given as zero.

→ The observed value of SPT from field requires some corrections.

(i) Overburden correction

(ii) dilatancy correction / water table correction /
fine correction.

i) Overburden-Correction:-

→ This correction is mainly used in cohesionless soils or granular soils.

→ it is observed that on ↑ depth / effective overburden pressure
Confining pressure ↑.

→ Due to higher confining pressure at the larger depths, SPT number is over-estimated.

→ ⊕ But when confining pressure is less in loose soil or @ the smaller depths, then SPT-value is under-estimated.

→ So to magnify the SPT number overburden correction is used.

$$N_1 = N_0 \left[\frac{350}{70 + \sigma'} \right]$$

N_1 = Corrected value after overburden correction.

N_0 = observed value of SPT

σ' = overburden pressure at the test level.

Here ($\sigma' \neq 280 \text{ kN/m}^2$).

i) $\sigma' \geq 280 \text{ kN/m}^2$. Thus this correction is not used.

ii) dilatancy / water table / fine correction:-

→ This correction is applied in fine sand and silt when water table is present.

→ This correction shall be applied when water table is "at or above" the test level. If w_t is below the test level then this correction not reqd.

→ due to the dynamic action of hammer pore pressure resistance is developed which causes the SPT number to be over estimated. Therefore to reduce the SPT value this correction is reqd.

$$N_2 = 15 + \frac{1}{2} (N_1 - 15)$$

($N_2 > 15$) @ always

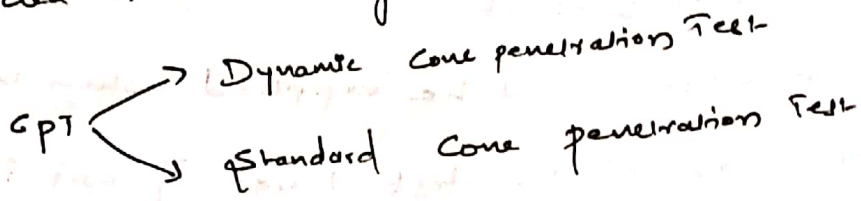
N_2 = final corrected value after w_t correction

N_1 = corrected value after over burden correction.

→ if $N_1 < 15$ then this correction is not reqd.

Cone-penetration-test: [CPT] →

CPT is divided into two types



Static Cone Penetration Test:

Rankine's Earth Pressure Theory:

Assumptions:

① ⇒ Soil is homogeneous & isotropic.

Homogeneous → Soil properties at every point is same
i.e. They should not vary with location
or with space.

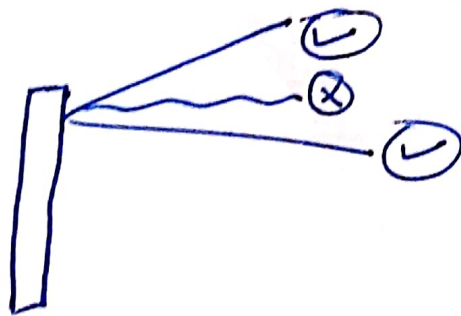
Isotropic → Prop. of soil is same in all-directions
i.e. soil prop. does not change with direction

② ⇒ Soil is cohesionless.

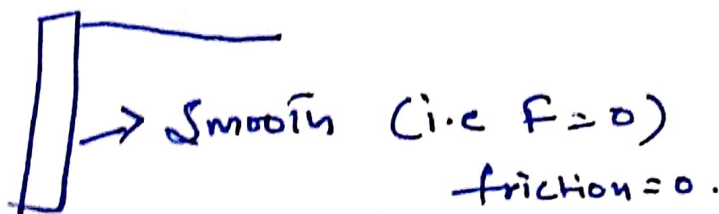
i.e. $c = 0$ (sandy).

some can say that R.E.P.T is applicable only
for cohesionless soils.

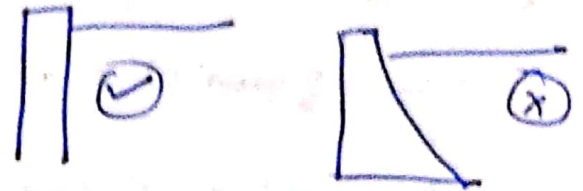
③ ⇒ Back fill surface near retaining structure should
be plane i.e. either horizontal or inclined.



④ ⇒ face of the R.W. in contact with the Back fill
should be considered as smooth



⑤ The face of wall in contact with Backfill
 \Rightarrow is vertical only.



⑥
 \Rightarrow The wall yields about its base such that the max values of c , ϕ are mobilised.

[i.e. if we study the failure of wall then we may have to calculate failure @ base. it may slide, overturn...]

@ failure $c_m, \phi_m = \phi_v, c_u$.

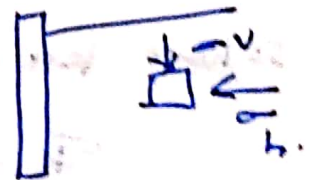
⑦
 \Rightarrow Elemental failure is considered.

[i.e. whenever we will calculate soil failure then we will calculate failure of each soil element]

Application of Rankine's Earth pressure theory:-

Active State:-

\rightarrow Let us take a small element of soil



σ_v & σ_h are vertical & horizontal forces acting on it.

\rightarrow as $\sigma_h < \sigma_v$ then

σ_h will be considered as Minor principle stress
 σ_v " " " " Major " "

so $\sigma_v' = \sigma_1$

$\sigma_h' = \sigma_3$

→ from Shear strength Theory

$$\sigma_1 = \sigma_3 \tan^2 \theta + 2c \tan \theta$$

$$\sigma_v' = \sigma_h' \tan^2 (45 + \phi/2) + 2c \cot(\tan \phi)$$

$$\sigma_v' = \sigma_h' \tan^2 (45 + \phi/2)$$

$$\sigma_v' = \sigma_h' \times (ka) \rightarrow \text{known } \Sigma \sigma$$

$$ka = \frac{\sigma_h'}{\sigma_v'} = \frac{1}{\tan^2 (45 + \phi/2)}$$

$$ka = \frac{1 - \sin \phi}{1 + \sin \phi}$$

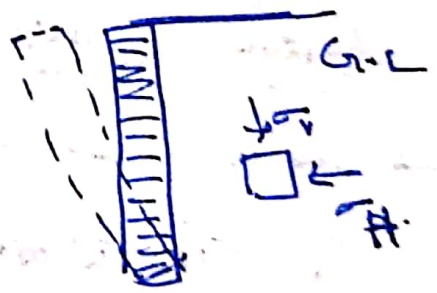
$$\sigma_h = ka \times \sigma_v \quad \text{here } ka = \frac{1 - \sin \phi}{1 + \sin \phi}$$

so here $ka < 1$ so

$$\sigma_H < \sigma_v$$

so $\sigma_H =$ Minor principle stress

$\sigma_v =$ Major principle stress.



above $\Sigma \sigma$ came from original $\Sigma \sigma$.

$$\sigma_3 = \sigma_1 \left[\frac{1 - \sin \phi}{1 + \sin \phi} \right] - 2c \sqrt{\frac{1 - \sin \phi}{1 + \sin \phi}}$$

$$\sigma_H = ka \sigma_v - 2c \sqrt{ka}$$

if $c=0$ then

$$\sigma_H = ka \sigma_v$$

∴ passive case:-

$$\sigma_H = K_p \times \sigma_v$$

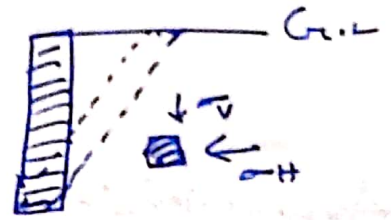
$$K_p = \frac{\sigma_H}{\sigma_v}$$

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi}$$

$$K_p > 1$$

So $\sigma_H > \sigma_v$

$$\sigma_H = \sigma_v, \quad \sigma_v = \frac{\sigma_v}{3}$$



Original σ_v

$$\sigma_v = \frac{\sigma_v}{3} \left[\frac{1 + \sin \phi}{1 - \sin \phi} \right] + 2c \sqrt{\frac{1 + \sin \phi}{1 - \sin \phi}}$$

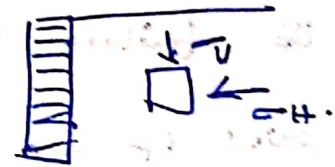
$$\sigma_H = K_p \times \sigma_v + 2c \sqrt{K_p}$$

$$K_p = \frac{\sigma_H}{\sigma_v} = \frac{1 + \sin \phi}{1 - \sin \phi}$$

@ Rest condition:-

$$\sigma_H = K_0 \times \sigma_v$$

$$K_0 = 1 - \sin \phi$$

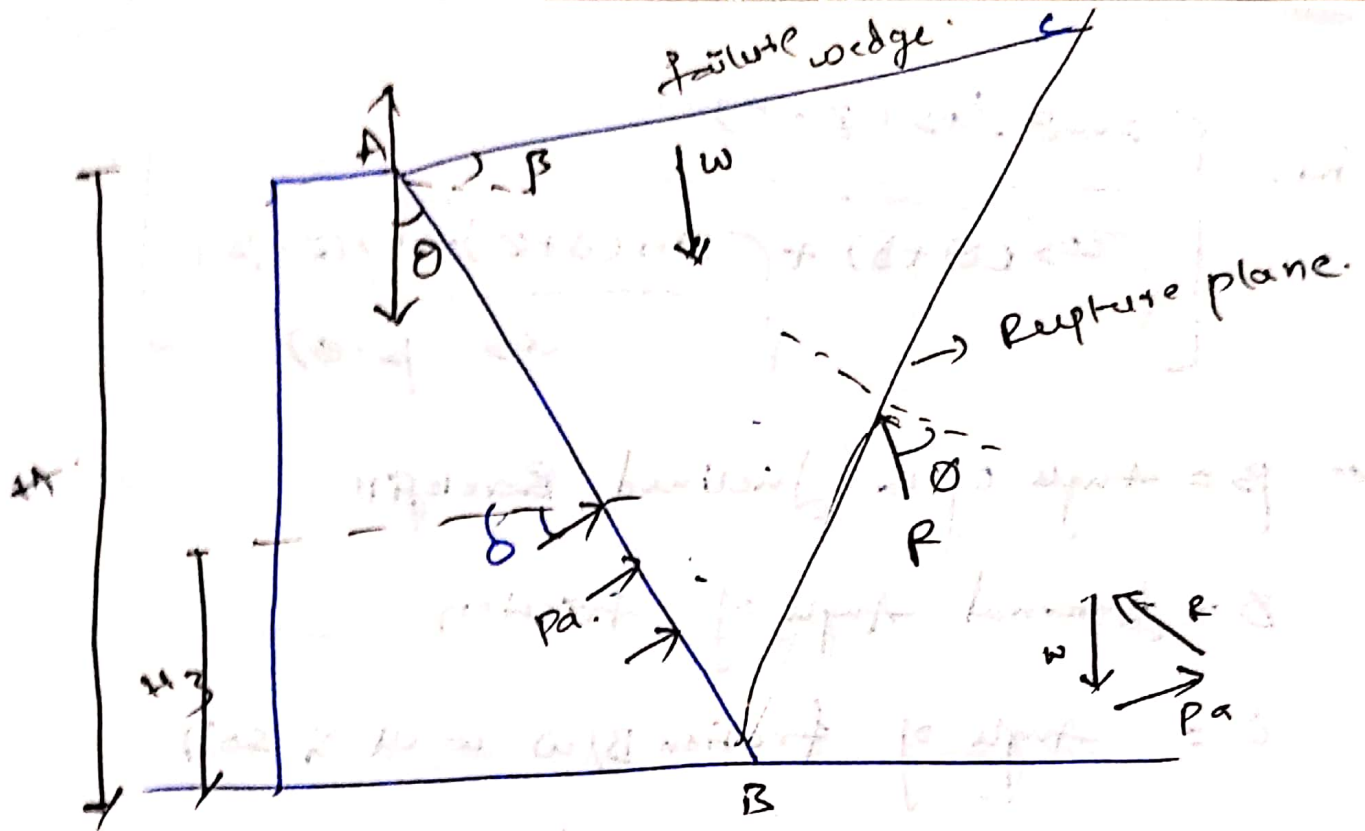


Columb's Earth pressure Theory (or)

Wedge Theory

Assumptions:-

- ① Soil is homogeneous, isotropic, infinite, plastic, dry, cohesionless.
- ② The face of wall in contact with back fill is vertical or inclined & it is rough.
- ③ The failure wedge acts as a rigid body & stresses over it are uniformly distributed.
- ④ The failure is essentially 2-D & rupture surface is planar & passes through the heel of the wall.
- ⑤ The location & direction of resultant thrust-
Blw wall & soil is known. The point of application is taken @ lower third point of the wall
By assuming triangular distribution of earth pressure.



- ② wedge failure is considered which is under equilibrium of 3 force.
- i) Self wt. of wedge ABC (w) Acting vertically downward direction.
 - ii) Resultant- Reaction R , acts @ downward angle of δ with Normal to Slip plane.
 - iii) Resultant- Reaction ' P_a ' Between the wall & soil acts @ a downward angle of δ with Normal of the wall.

$$K_a = \left[\frac{\sec \theta \cdot \cos(\phi - \theta)}{\sqrt{\cos(\theta + \delta)} + \sqrt{\frac{\sin(\delta + \theta) \cdot \sin(\phi - \beta)}{\cos(\beta - \theta)}}} \right]^2$$

Here $\beta =$ Angle of the Inclined Backfill

$\theta =$ Internal Angle of friction

$\delta =$ Angle of friction b/w wall & soil

(generally assumed as $\frac{2}{3}\theta$)

$\theta =$ Angle made by vertical with inclined face.

Note: if wall is vertical ($\theta = 0^\circ$), Horizontal Backfill ($\beta = 0$), if wall is smooth ($\delta = 0$)

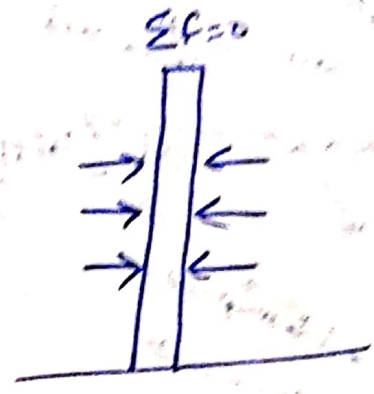
Then

$$(K_a)_{\text{Coulomb}} = (K_a)_{\text{Rankine}}$$

Earth pressure @ Condition:

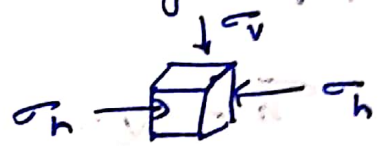
$\Sigma F =$ Net-force.

if $\Sigma F = 0$ wall will not move.



$$k_0 = \frac{\sigma_h}{\sigma_v}$$

So net change in vol of soil = 0.



$$\left(\frac{\Delta v}{v_0}\right) = 0 \text{ i.e. volumetric strain} = 0.$$

So from some work

$$\frac{\sigma_h}{E} - \mu \frac{\sigma_h}{E} - \frac{\mu \sigma_v}{E} = 0$$


$$\sigma_h (1 - \mu) = \mu \sigma_v$$

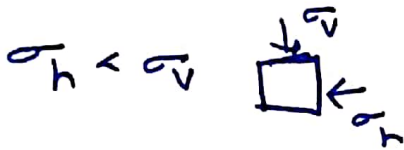
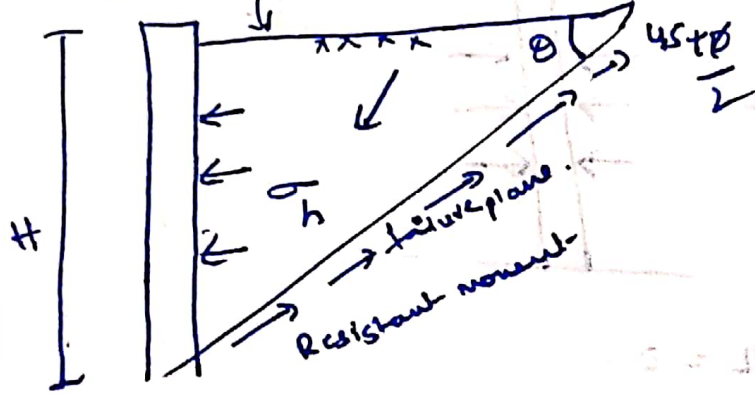
$$k_0 = \frac{\sigma_h}{\sigma_v} = \frac{\mu}{1 - \mu}$$

$\mu =$ poisson's Ratio.

for sandy soil $k_0 = 1 - \sin \phi$

for o.c. clay $(k_0)_{oc. clay} = (k_0)_{nc. clay} \times \sqrt{OCR}$

active  major principle plane. soil moment downward



$\sigma_h = \text{minor} = \sigma_3$
 $\sigma_v = \text{Major} = \sigma_1$

from shear stresses

Angle b/w failure plane & major principle plane.

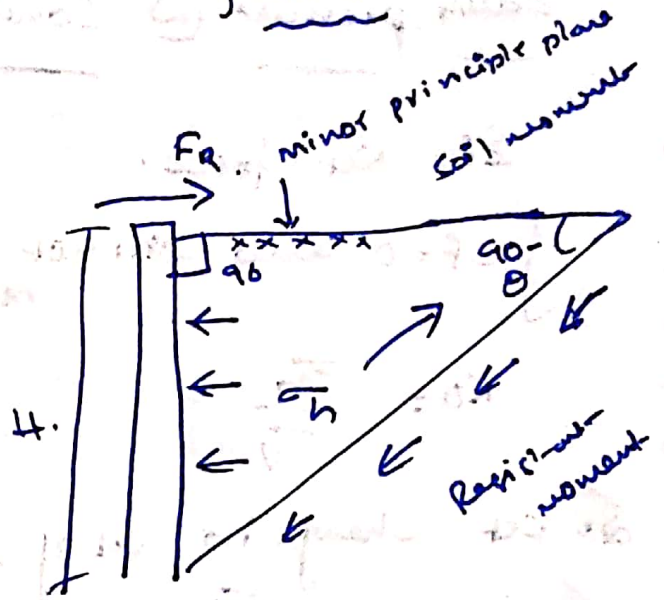
$$\theta = \frac{\pi}{4} + \frac{\phi}{2}$$

$$\tan \theta = \frac{H}{L_a}$$

$$L_a = H / \tan \theta$$

$$L_a = H \cot \theta$$

passive



$\sigma_h > \sigma_v$

$\sigma_h = \text{major} = \sigma_1$
 $\sigma_v = \text{minor} = \sigma_3$

$$90 - \theta$$

$$90 - (45 + \frac{\phi}{2})$$

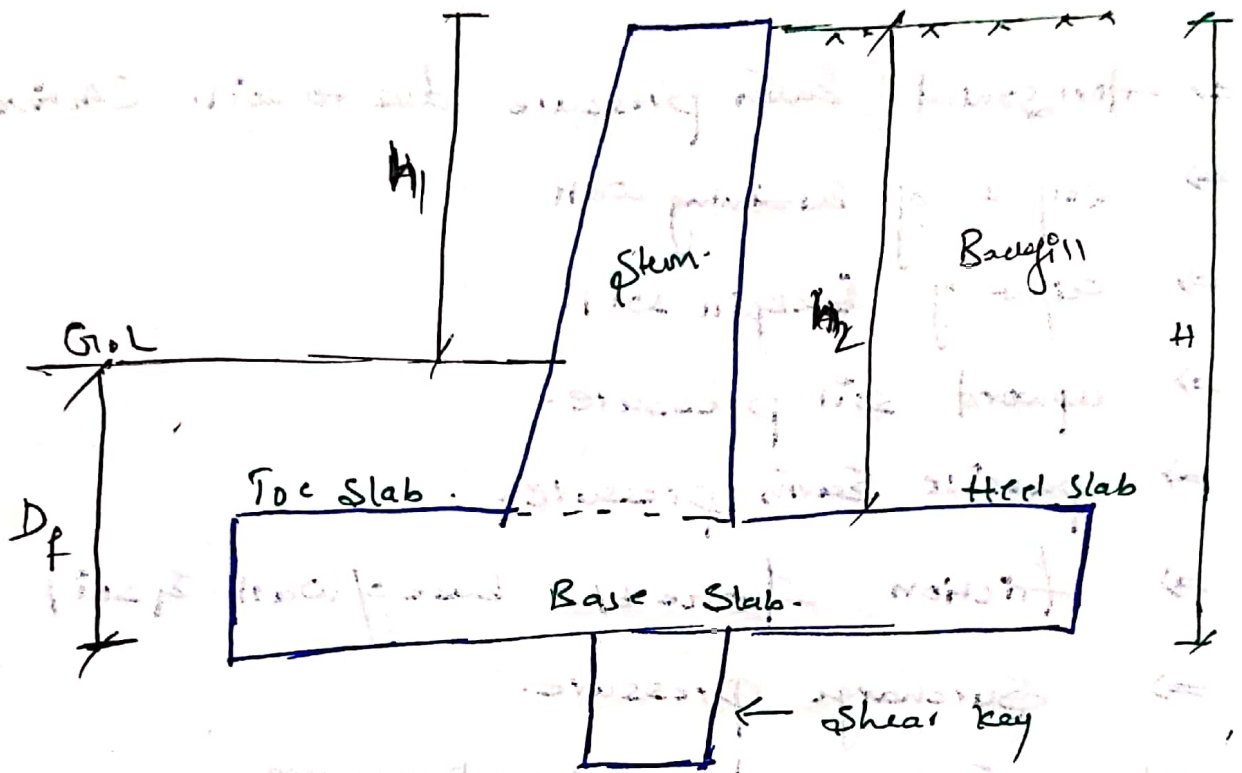
$$= 45 - \frac{\phi}{2}$$

$$L_b = H \cot \theta (90 - \theta)$$

$$= H \cot (45 - \frac{\phi}{2})$$

$$L_p > L_a$$

Stability checks for R.W. :-



⇒ Stem can be rectangular or Trapezoidal.

H = Total height of R.W.

h_2 = Height of stem above & below G.L.

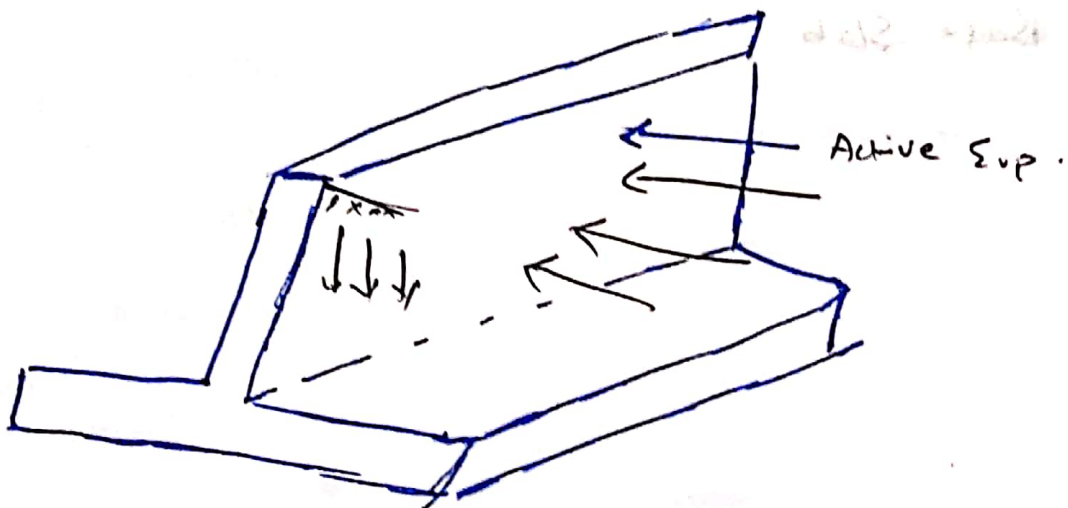
h_1 = " " R.W. above G.L.

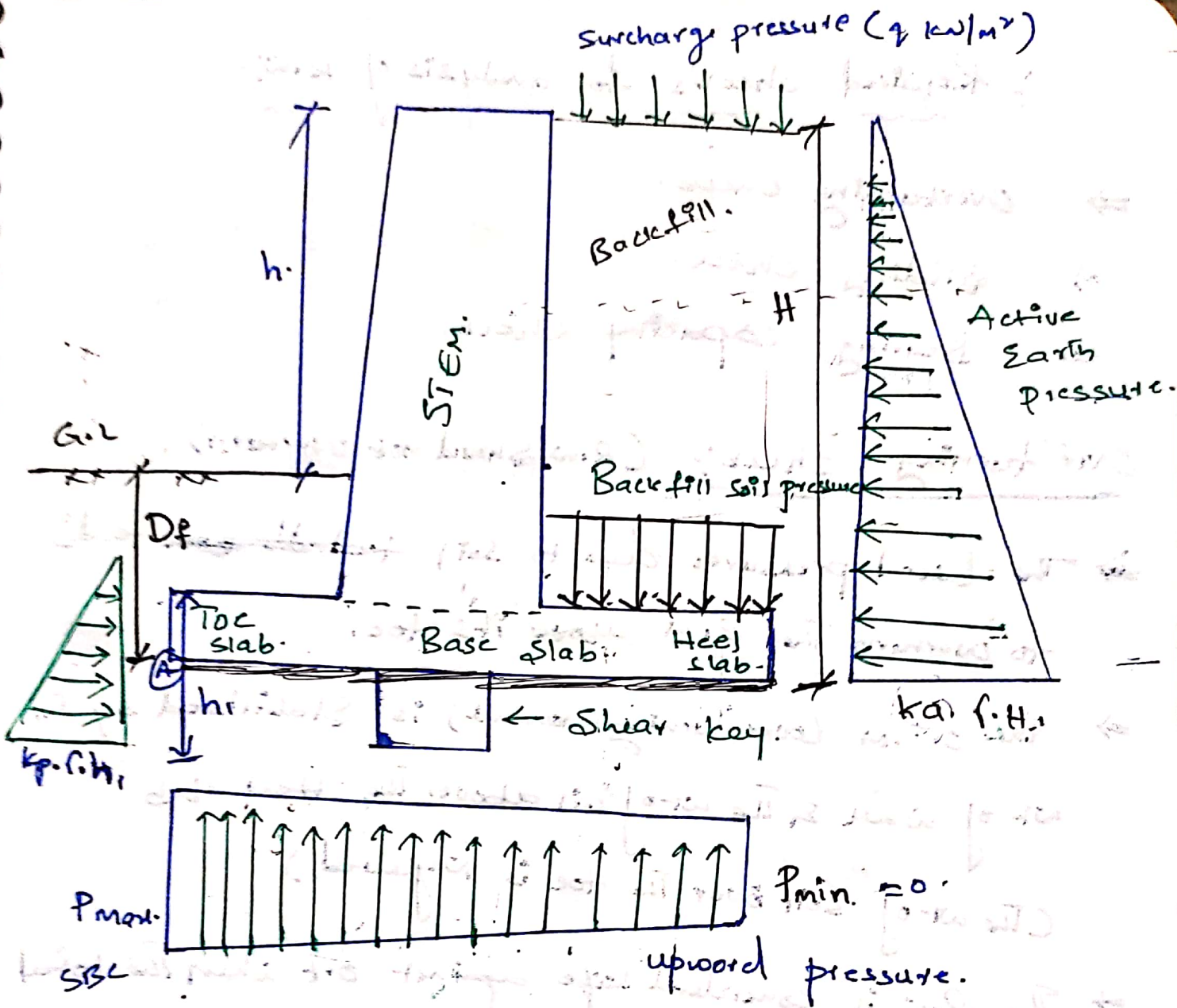
D_f = D_f = Depth of foundation from below G.L. to End of Base Slab.



Forces acting on Retaining wall:-

- ⇒ Horizontal Earth pressure due to soil. (Active E.P)
- ⇒ Self wt of Retaining wall
- ⇒ weight of backfill soil.
- ⇒ upward soil pressure.
- ⇒ passive Earth pressure.
- ⇒ Friction force b/w base of wall & soil
- ⇒ Surcharge pressure.
- ⇒ Submerged water pressure.





$$k_a = \frac{1 - \sin \theta}{1 + \sin \theta} \quad k_p = \frac{1 + \sin \theta}{1 - \sin \theta}$$

θ = Angle of Internal friction of soil!

As per formula $k_a = \frac{1}{k_p}$

∴ Required checks for analysis of R.W.:-

- ⇒ Overturning check.
- ⇒ Sliding check.
- ⇒ Bearing capacity check.

Overturning check:- (R.W. should not overturn).

⇒ The lateral pressures due to soil ~~tends to~~ tend to overturn the R.W. above its toe.

⇒ The O.T.M (Overturning moment) is stabilised by the wt of wall & the wt of soil above the heel slab (The wt of soil over the toe is neglected).

⇒ The R.W. is considered safe against O.T. when the total stabilizing or resisting moment is at least 100% greater than the O.T.M.

Overturning check:-

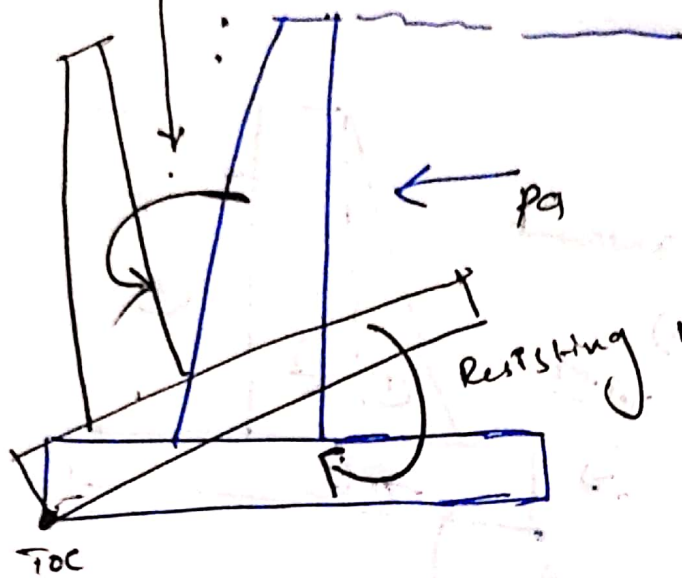
$$\text{Fos of overturning} = \frac{\text{Resisting moment}}{\text{overturning moment}}$$

Resisting moment = Moment due to vertical forces ^(down ward)

Overturning moment = Moment due to H₃ forces.

$$\text{Fos overturning} \geq 1.5$$

overturning moment



Horizontal forces: (Lateral forces):

Active Earth pressure (P_a) = area of active pressure triangle

$$= \frac{1}{2} \times (K_a \cdot f \cdot H) \times H$$

$$= \frac{1}{2} \times K_a \cdot f \cdot H^2$$

Moment of point A = overturning moment, M_o (Anticlockwise)

Moment = Force \times Per dist

Force \times Per dist

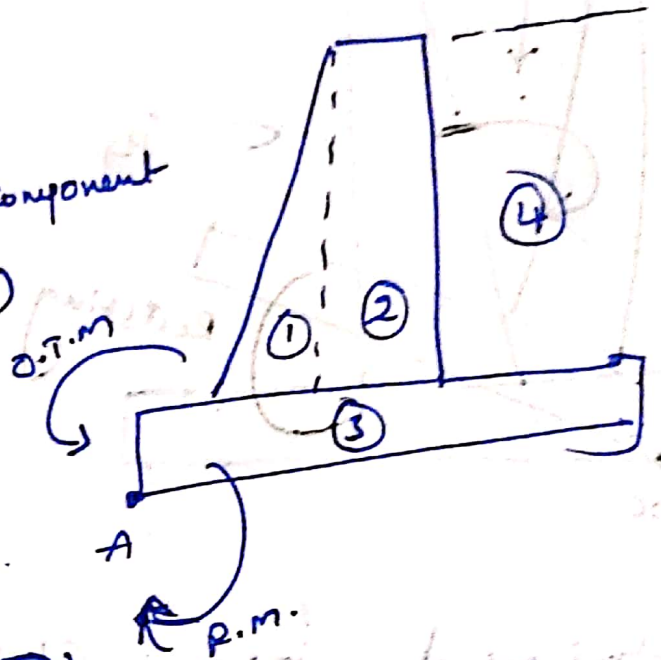
$$\Rightarrow P_a \times H/3$$


$$\Rightarrow \frac{1}{2} \times K_a \times f \cdot H^2 \times \frac{H}{3}$$

Vertical forces: (downward forces):-

i) pressure due to Back fill

ii) Self wt of R.W. (Area of component $1+2+3+4$)



Self wt of R.W. = Total wt of 

diff components of R.W

Downward force due to Back fill soil =

total wt of back fill soil

Moment @ joint-A = Resisting Moment - M_R (clockwise)

= Force \times Per dist

ΣV = total vertical forces =

Sliding check:

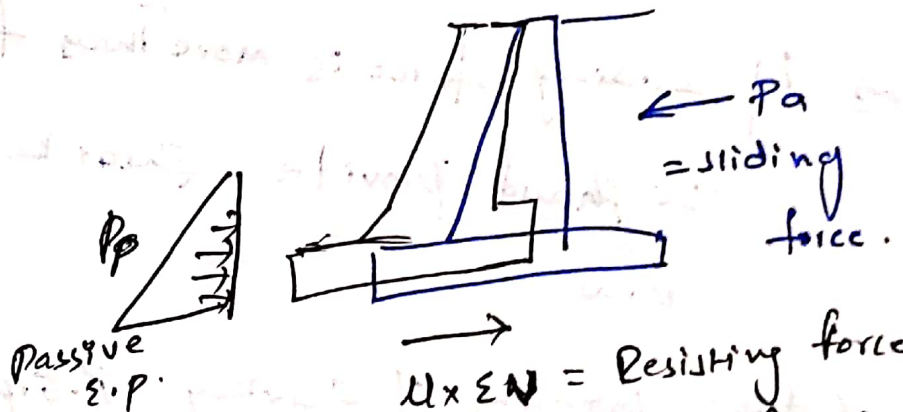
$$\text{Fos of Sliding} = \frac{\text{Resisting force}}{\text{sliding force}}$$

$$\frac{(\mu \Sigma V + P_p)}{P_{ah}} > = 1.55$$

Sliding force = P_a = horizontal component

Resisting force = $\mu \times \Sigma V + P_p$

P_p = passive force.



μ = co. of friction

ΣV = sum of total vertical force.

Sliding check:-

- The lateral E.P on stem tries to slide the R.W away from back fill soil. Such force exert on R.W considered as sliding force.
- Resting lateral force is acting from opposite direction such resisting force is considered as "frictional force".
- Eventually sliding force can be resisted by friction force which is generated b/w Base of wall & soil.
- if sliding force is more than frictional force, we should provide shear key @ the bottom of R.W.

(due to providing of shear key P.E.P ↑)

* Bearing Capacity Check:

- ⇒ Soil pressure acts on the Bottom of the wall from downward to upward
- ⇒ it varies linearly with more pressure on toe side & less pressure on heel side.
- ⇒ These upward soil pressure should not be more than SBC of soil & it should not less than zero.
- ⇒ To satisfy this criteria, middle third rule should be satisfy....
- ⇒ As per middle third rule, the resultant forces of the forces from R.W, it should be fall within middle third portion
- ⇒ if we can't satisfy middle third rule, should change size of R.W.
- ⇒ Eventually due to upward pressure of soil, the base of wall should be in compression

$$P_{max} = \frac{EV}{A} + \frac{M}{Z} < SBC$$

$$P_{min} = \frac{EV}{A} - \frac{M}{Z} \geq 0.$$

Here $M = \Sigma V \cdot e$.

ΣV = total vertical forces

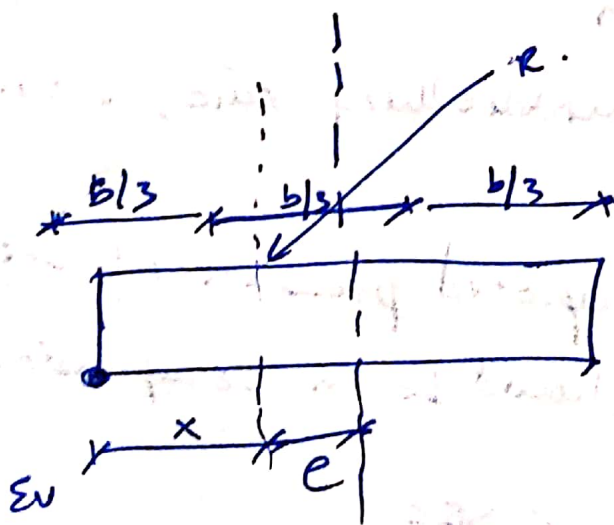
e = Eccentricity of Resultant forces from TOC.

A = Base Area of retaining wall.

∴ Middle Third rule:

⇒ If the Resultant force acts within the middle third, the Bearing pressure diagram is trapezoidal & 100% of the Base will be in Compression

⇒ $P_{max} < SBC$, if it will more than SBC then RW Bas will be fail

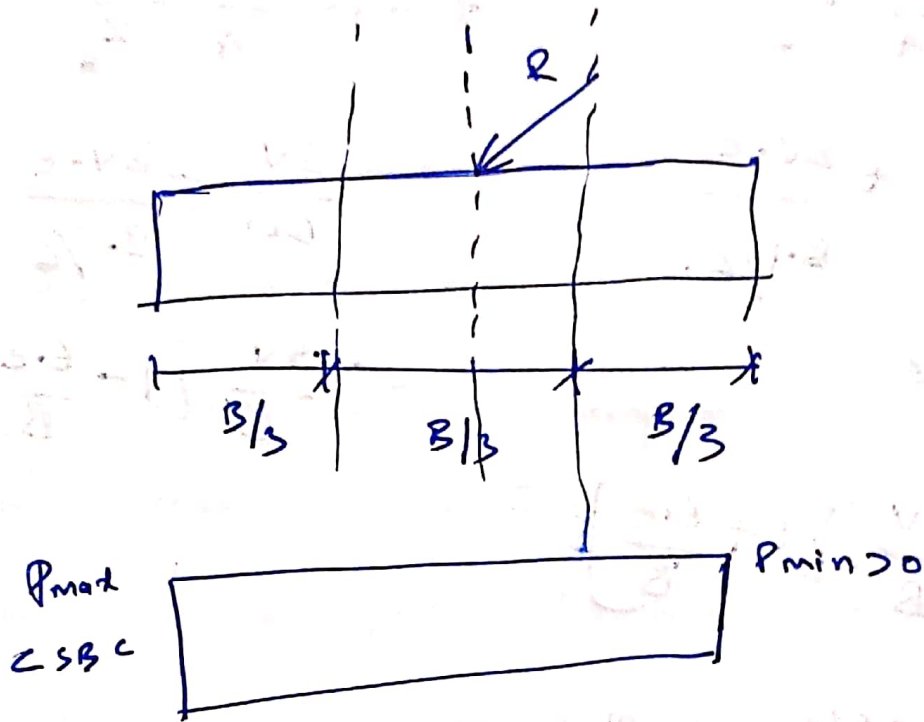


e = eccentricity from center of Base to the dist. b where resultant force is acting.

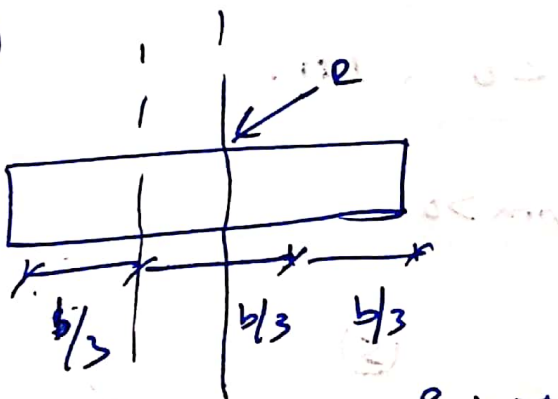
Here $x = \frac{\Sigma \text{moment about TOC}}{\Sigma V}$

$$x = \frac{M_x - M_0}{\Sigma V}, \quad e = \frac{b}{2} - x$$

middle third portion.

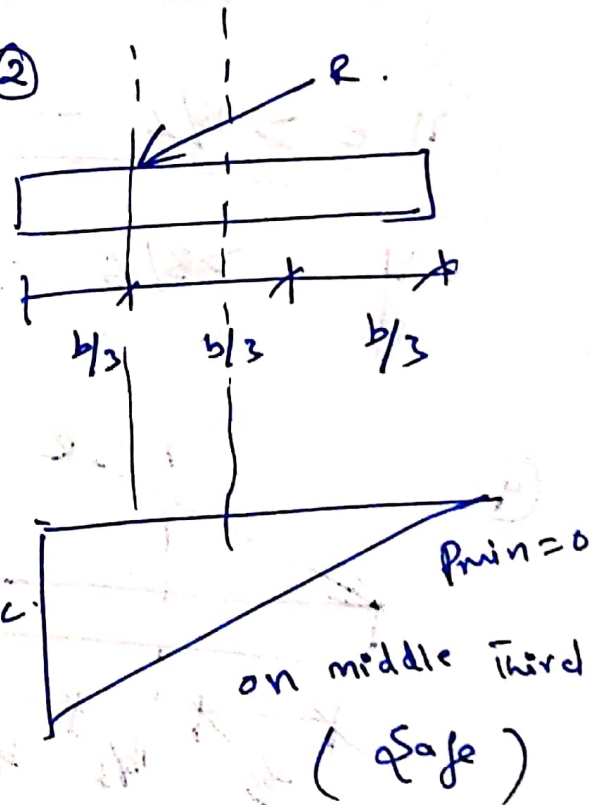


①



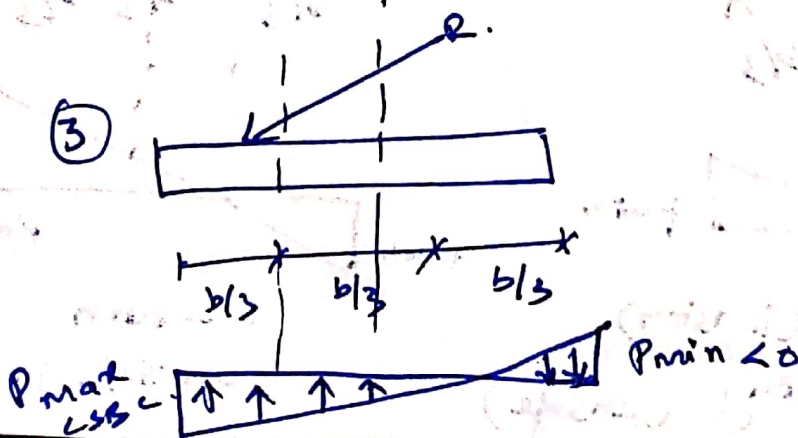
P_{max}
 $< SBC$
within middle third (safe)

②



$P_{max} < SBC$
on middle third
(safe)

③



(un-safe)
(outside of middle third)

$$P_{max} = \frac{\Sigma V}{A} + \frac{M}{Z}$$

$$= \frac{\Sigma V}{B \times l} + \frac{\Sigma V \cdot e}{B \cdot l/6}$$

$$P_{min} = \frac{\Sigma V}{A} - \frac{M}{Z}$$

$$= \frac{\Sigma V}{B \times l} - \frac{\Sigma V \cdot e}{B \cdot l/6}$$

ln length of way
B = width

$$= \frac{\Sigma V}{B} \left[1 - \frac{6 \cdot e}{B} \right]$$

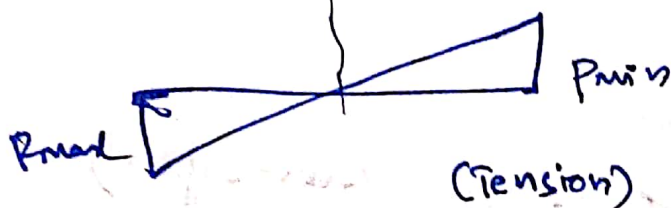
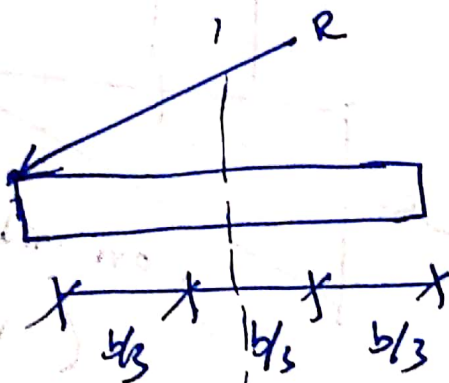
$$\Rightarrow \frac{\Sigma V}{B} \left[1 + \frac{6 \cdot e}{B} \right]$$

if $e = B/6$ -- $P_{min} = 0$

if $e > B/6$ -- $P_{min} < 0$ Let.

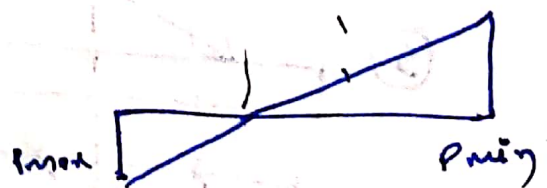
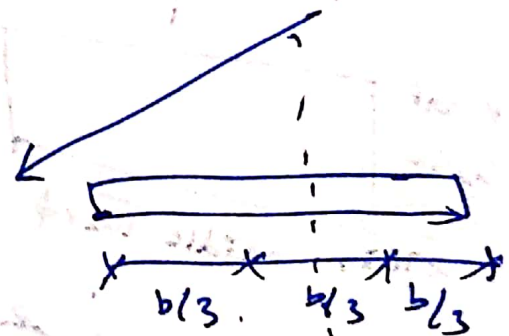
if $e < B/6$ -- $P_{min} > 0$

④



On- verge of over turning. (Unsafe)

⑤



(un-safe).

Example problems for cohesion-less soils:-

Here we have 4 types of problems

- ① Earth pressure in general case \Rightarrow with vertical wall & horizontal backfill [Dry or moist soil without surcharge]
- ② Earth pressure with surcharge with horizontal backfill
- ③ Earth pressure with inclined backfill & surcharge.
- ④ Effect of submerged soil Earth pressure with horizontal backfill.

Case - I

Earth pressure in general case - with vertical wall and horizontal backfill (dry or moist-soil without surcharge)

Check the stability of cantilever L.W which is used to support a bank of earth 4m height above G.L.

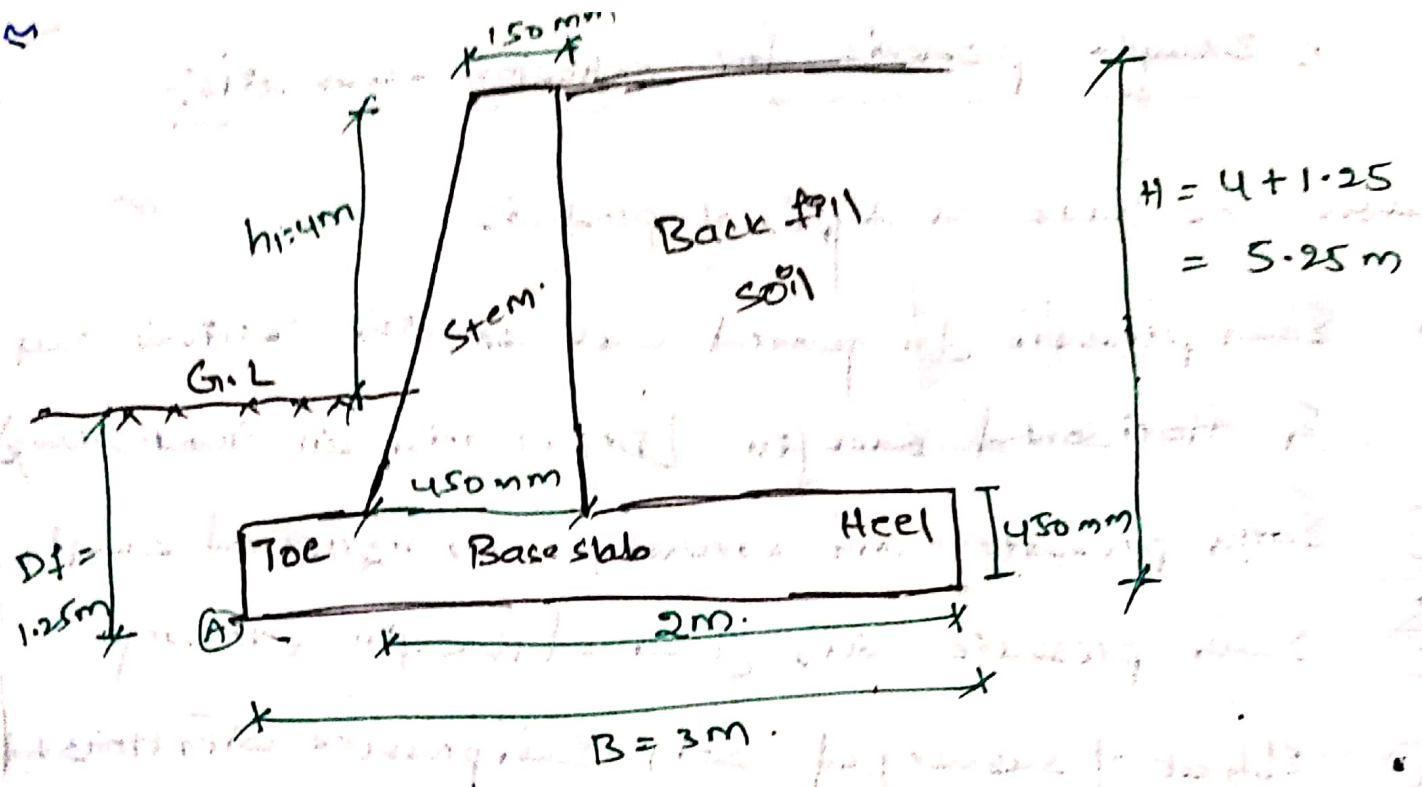
Dimensions of Row are given in Diagram.

\Rightarrow Assume S.B.C of soil is 160 kN/m^2

\Rightarrow U.W of soil is 16 kN/m^2

\Rightarrow Angle of internal friction of soil is 30°

\Rightarrow coefficient of friction b/w concrete & soil is 0.5 use M25 & FC415



Soln:- We know $k_a = \frac{1 - \sin \phi}{1 + \sin \phi}$ & $k_p = \frac{1 + \sin \phi}{1 - \sin \phi}$

Given $\phi = 30^\circ$ (Angle of internal friction)

So $k_a = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ}$, $k_p = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ}$

$k_a = \frac{1}{3}$

$k_p = 3$

Overturning check:-

Fos of overturning = $\frac{\text{Resisting moment } (M_R)}{\text{Overturning moment } (M_o)}$

M_R = Moment due to vehicle forces (down ward)

M_o = Moment due to Hz forces

Fos. of overturning > 1.5

Soln:-

$$k_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

$$k_p = \frac{1 + \sin \phi}{1 - \sin \phi}$$

Given $\phi = 30^\circ$

$$k_a = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ} = \frac{1}{3}$$

$$k_p = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ} = 3$$

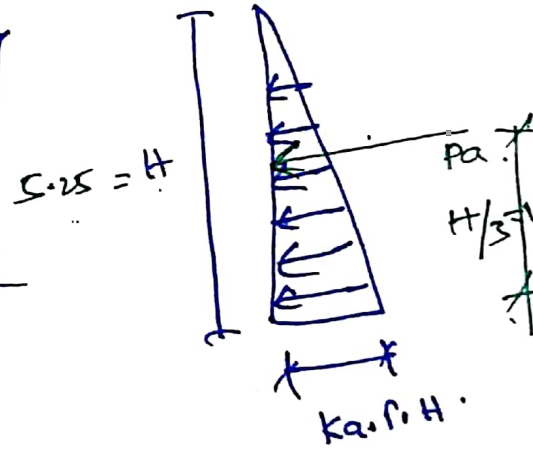
① check for Overturning:-

$$Fos = \frac{\text{Resisting Moment (MR)} \Rightarrow \text{vertical forces } (\downarrow)}{\text{Overturning moment (MO)} \Rightarrow \text{H}_2 \text{ forces } (\leftarrow)}$$

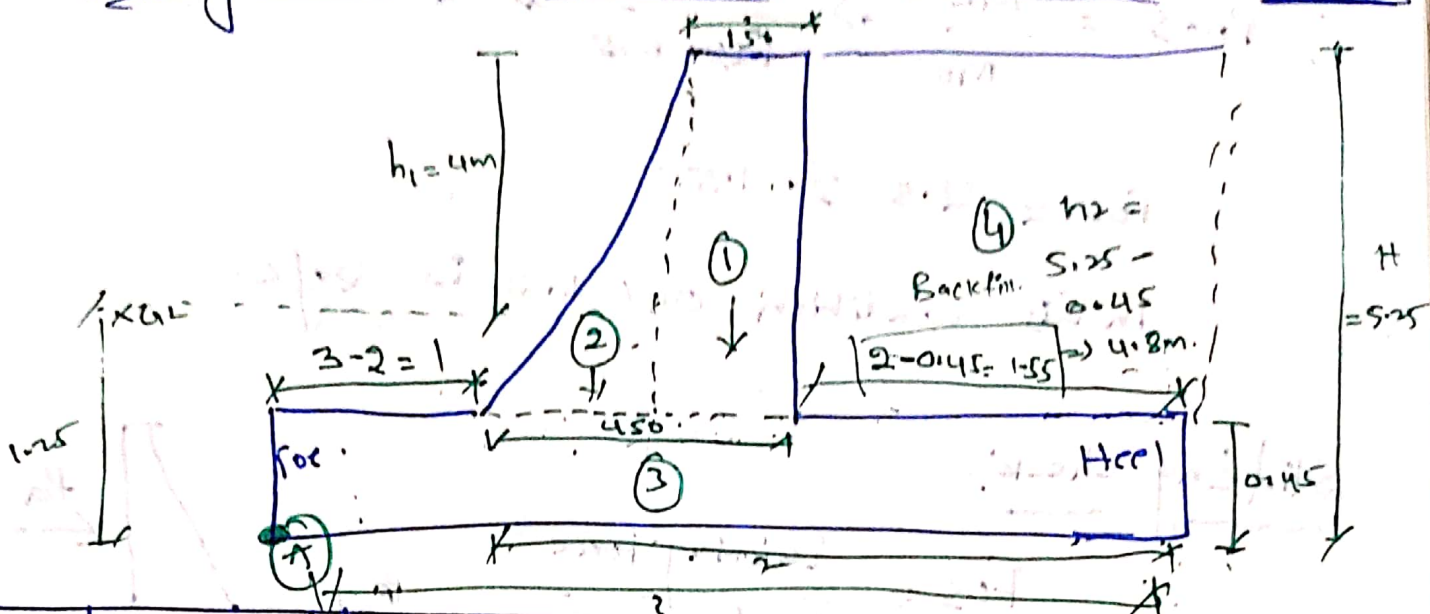
Overturning moment (MO) \Rightarrow (due to H₂ forces).

H₂ forces \Rightarrow Pa = lateral earth pressure.

force (Pa)	Distance from Bottom	Moment
\Rightarrow Area of Triangle		
$\Rightarrow \frac{1}{2} \times \text{Base} \times \text{Height}$	$\frac{H}{3}$	force \times Le _{dist}
$\Rightarrow 0.5 \times (k_a \cdot \rho \cdot H) \times H$	$\Rightarrow \frac{5.25}{3}$	$\Rightarrow 73 \times 1.75$
$\Rightarrow 0.5 \times \frac{1}{3} \times 16 \times (5.25)^2$	$\Rightarrow 1.75$	$\Rightarrow 128.625$
$\Rightarrow 72.765$		≈ 128



Resisting moments = Moment due to vertical forces (\downarrow direction)



Element no	Name of element	force/load (kN) Self wt of element \Rightarrow vol of element \times density of material	Distance from point (A) (m)	Moment about point (A)
1	Stem = Rectangle	$(0.15 \times 4.8 \times 1) \times 25 = 18$	$(\frac{0.15}{2}) + (0.45 - 0.15) + 1 \Rightarrow 1.375$	force \times dist $18 \times 1.375 \Rightarrow 24.75$
2	Stem = triangle	$[\frac{1}{2} (0.45 - 0.15) \times 4.8] \times 25 = 18$	$\frac{2}{3} (0.3) + 1 \Rightarrow 1.2$	$18 \times 1.2 \Rightarrow 21.6$
3	Base of slab	$(1 \times 0.45 \times 3) \times 25 = 33.75$	$\Rightarrow \frac{B}{2} = \frac{3}{2} \Rightarrow 1.5$	$\Rightarrow 33.75 \times 1.5 \Rightarrow 50.62$
4	Backfill material	$[1 \times (2 - 0.45) \times 4.8] \times 16 = 119.04$	$\Rightarrow 1 + 0.45 + (\frac{1.55}{2}) \Rightarrow 2.225$	$119.04 \times 2.225 \Rightarrow 264.84$
5	Shear key	$(1 \times 0.45 \times 0.3) \times 25 \Rightarrow 5.62$	$1 + (\frac{0.45}{2}) \Rightarrow 1.225$	$\Rightarrow 5.62 \times 1.225 \Rightarrow 6.89$
		$\Sigma V = 188.79 \text{ kN}$		$\Sigma M_1 = 361.839 \text{ kNm}$
		$\Sigma V_2 = 188.79 + 5.62 \Rightarrow 194.41$		$\Sigma M_2 = 361.839 + 6.89 \Rightarrow 368.73$

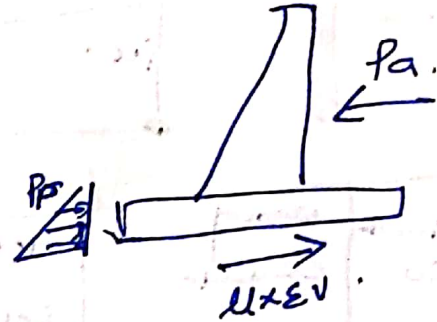
$$FOS = \frac{MR}{M_0} \Rightarrow \frac{361.89}{128.625} \Rightarrow 2.8$$

$$FOS = 2.8 > 1.5$$

In this condition our F.O.S is safe.

Sliding check:-

$$FOS = \frac{\text{Resisting force}}{\text{sliding force}}$$



$$FOS = \frac{(U \times EV + PP)}{Pa}$$

$Pa =$ horizontal component / A.E.P.

Resisting force $\Rightarrow U \times EV + PP$. ($PP = P \cdot E \cdot P$)

$$Pa = \frac{1}{2} \times \text{Base} \times \text{height} \Rightarrow \frac{1}{2} \times (ka \times r \times H) \times H$$

$$= \frac{1}{2} \times ka \times r \times H^2$$

$$\Rightarrow 0.5 \times \frac{1}{3} \times 16 \times (5.25)^2$$

$$\Rightarrow \underline{73.5 \text{ kN}}$$

$$PP = \left(\frac{1}{2} \times \text{base} \times \text{height} \right) \Rightarrow \frac{1}{2} \times (k_p \times r \times 0.45) \times 0.45$$

$$\Rightarrow \frac{1}{2} \times 3 \times 16 \times (0.45)^2$$

$$\Rightarrow 4.86 \text{ kN}$$

$$\Sigma V = 188.79$$

$$FOS = \left(\frac{4 \times \Sigma U + P_p}{P_a} \right)$$

$$\Rightarrow \frac{(0.5 \times 188.79) + 4.26}{73.5}$$

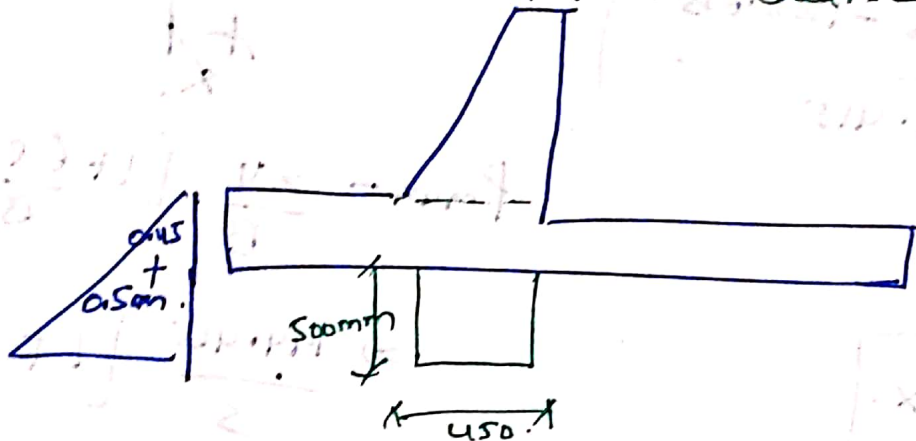
$$\Rightarrow \left(\frac{99.26}{73.5} \right) \Rightarrow 1.35$$

FOS for sliding is 1.55

But we got FOS < 1.55 i.e. 1.35

So our D.W is un-safe.

So we should provide - Shear-key



after providing shear key ΣU change.

& passive Σp is also changes

$$P_a \Rightarrow \left(\frac{1}{2} \times \text{Base height} \right) \times \text{height}$$

$$\Rightarrow \frac{1}{2} \times (K_p \times r \times 0.9) \times 0.9$$

$$P_p \Rightarrow 0.5 \times (3 \times 16 \times 0.95) \times 0.95 \Rightarrow 21.66 \text{ kN}$$

$$\text{Resisting force. } \left[(0.5) \times (194.415) \right] + 21.66$$

$$\Rightarrow 94.39 + 21.66 \Rightarrow 118.86 \text{ kN}$$

$$FOS = \frac{118.86}{73.5} \Rightarrow 1.61$$

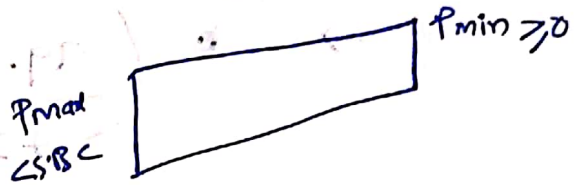
$$1.61 > 1.55$$

So. D.W. is safe.

Check for B.C

$$P_{max} = \frac{\Sigma V}{B} \left[1 + \frac{6e}{B} \right] < SBC$$

$$P_{min} = \frac{\Sigma V}{B} \left[1 - \frac{6e}{B} \right] \geq 0$$



$$X = \frac{\Sigma \text{Moment about toe}}{\Sigma V}$$

$$X = \frac{M_r - M_o}{\Sigma V}$$

$$X = \left(\frac{368.98 - 128.625}{194.415} \right)$$

$$X = 1.23$$

$$e = \frac{B}{2} - X$$

$$e = \frac{3}{2} - 1.23$$

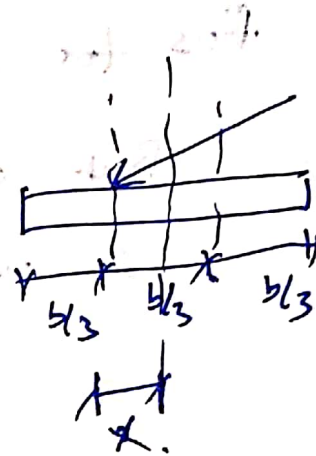
$$\Rightarrow 1.5 - 1.23$$

$$e \Rightarrow 0.27$$

$$e < B/6$$

$$0.27 < \frac{3}{6}$$

$$\Rightarrow 0.27 < 0.5$$



$$P_{max} = \frac{\Sigma V}{B} \left[1 + \frac{6e}{B} \right]$$

$$\Rightarrow \frac{194.415}{3} \left[1 + \frac{6 \times 0.27}{3} \right]$$

$$P_{max} \Rightarrow 99.79 < SBC$$

$$\Rightarrow 160$$

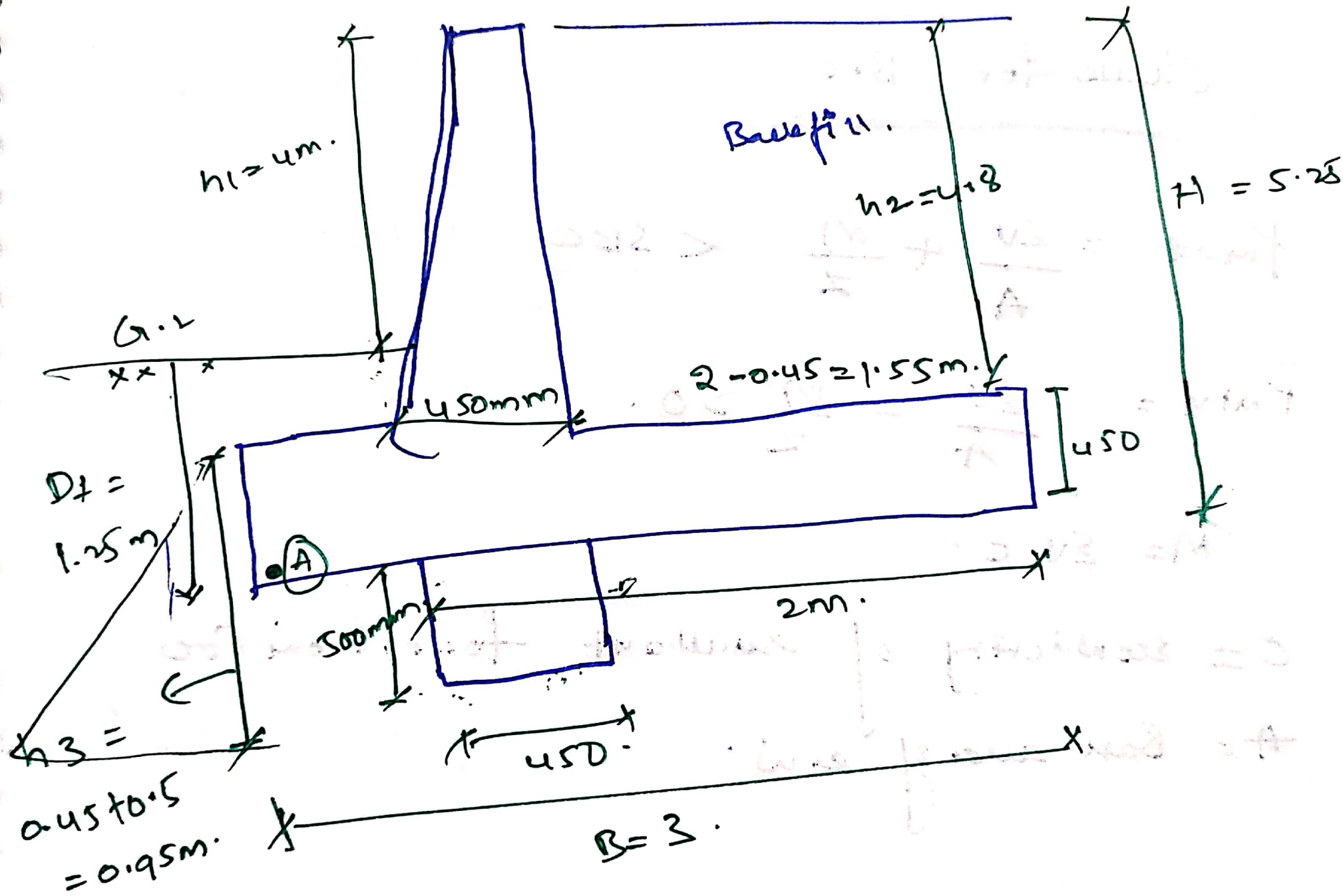
$$\Rightarrow 99.79 < 160 \text{ Safe}$$

$$P_{min} = \frac{\Sigma V}{B} \left[1 - \frac{6e}{B} \right]$$

$$\Rightarrow \frac{194.415}{3} \left[1 - \frac{6 \times 0.27}{3} \right]$$

$$P_{min} \Rightarrow 29.81 \text{ kN} \geq 0$$

Safe Condition.

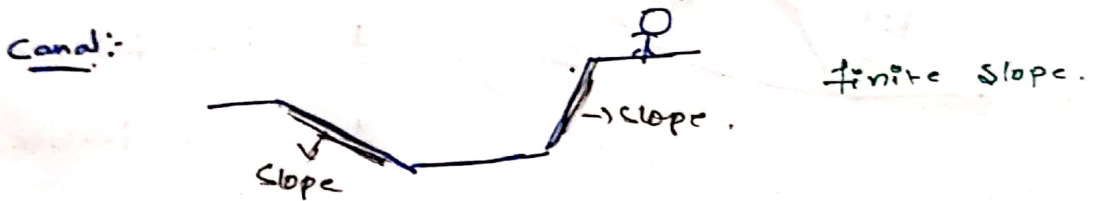
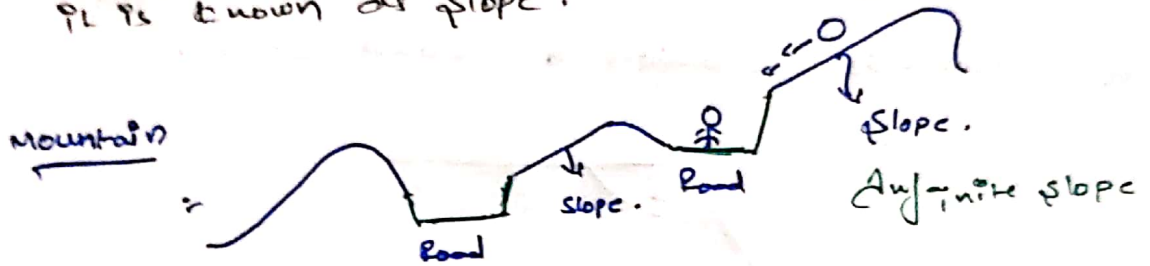


Module-2:-

Slope Stability & Earth Pressure Theories :-

Introduction:-

Slope:- When the soil is formed in inclined position then it is known as slope.



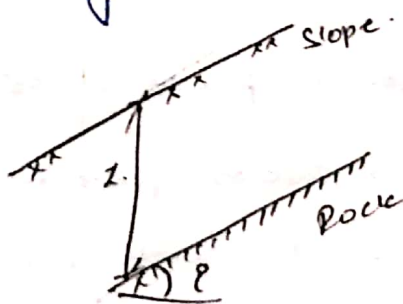
Slopes are Two types:-

- Infinite Slope
- finite Slope.

Infinite Slope:-

- ⇒ Infinite Slopes are not bounded. [Ex: Mountain]
- ⇒ failure surface is parallel to the surface of slope.

i.e



ϕ = Angle of slope.

- ⇒ on increasing the z value slope failure will occur i.e soil shear's

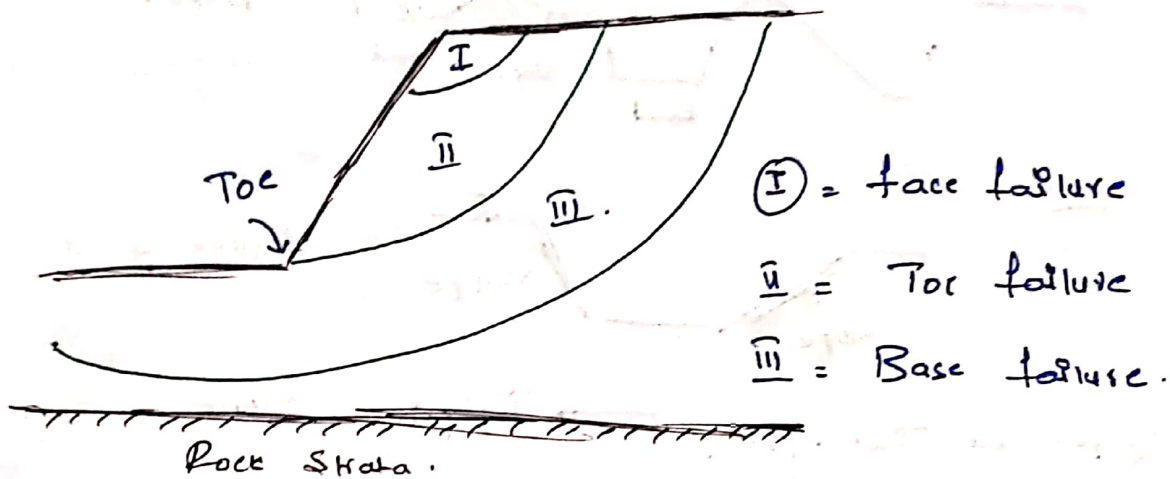
② finite Slopes:-

⇒ They are Bounded from Top & bottom. (Ex: canal)

⇒ failure Surface is circular or spiral.

⇒ ~~finite~~ finite Slopes are having different failure modes, unlike infinite Slopes.

to Explain this Consider a canal Section.



⇒ Face failure is occurred when the soil in the upper part is weaker than the soil of lower part. Thus weaker soil will shear's. Such failure is called face failure.

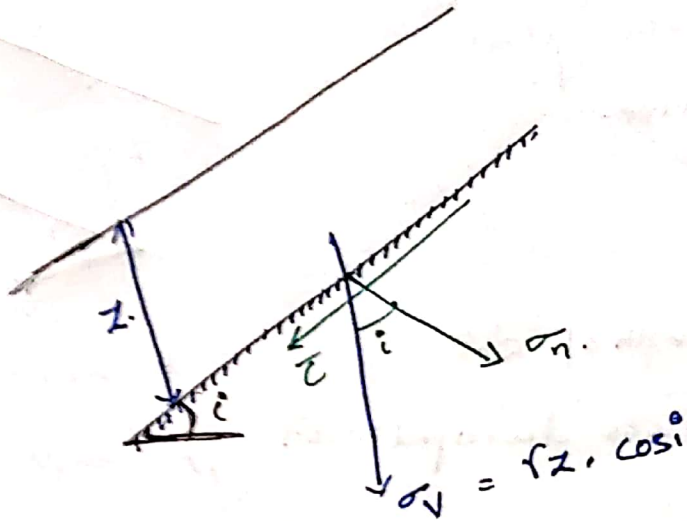
⇒ Toe-failure:-

whenever upper & lower parts of soil's are homogeneous then in that condition due to increasing in stresses the failure is occurred. such failure is called as Toe-failure.

⇒ Base-failure:- (opposite to face failure).

when the lower part of soil is weaker comparatively to the upper part of soil then Base-failure is occurred.

Analysis of Infinite Slope:-



σ_n = Normal Stress / Normal component

τ = Shear Stress or Tangential stress.

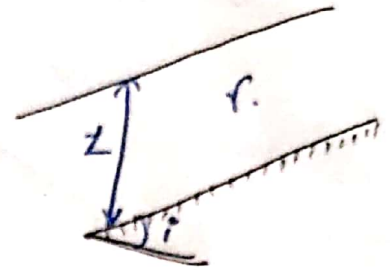
$$\sigma_n = \sigma_v \times \cos i \Rightarrow (rz \times \cos i) \times \cos i \Rightarrow$$

$$\tau = \sigma_v \times \sin i \Rightarrow rz \cos i \times \sin i \Rightarrow$$

$\sigma_n = rz \cos^2 i$
$\tau = rz \cos i \times \sin i$

Case-1: cohesion less soil on Anticlastic slope's (sandy soil)
 (NO-water Table condition)

⇒ Here we will calculate FOS against sliding/shear failure.



$$FOS = \frac{\tau_f}{\tau}$$

i.e. FOS = $\frac{\text{Shear strength of soil}}{\text{Shear stresses developed in soil}}$

ϕ - Angle of slope
 ϕ - Angle of internal friction

W.K.T $\tau_f = c' + \sigma' \tan \phi'$ from Mohr's column Theory

$$\text{So } FOS = \frac{\tau_f}{\tau} = \frac{c' + \sigma' \tan \phi'}{\tau}$$

$$FOS = \frac{0 + \sigma_n \tan \phi}{\tau}$$

$$FOS = \frac{\sigma_n \tan \phi}{\tau}$$

⇒ here $c=0$ BCS soil is cohesionless (sandy)
 ⇒ ϕ' becomes ϕ BCS NO pore water pressure

from Sum ① & ② W.K.T $\sigma_n = rz \cos^2 i$, $\tau = rz \cos i \times \sin i$

$$\text{So } FOS = \frac{(rz \cos^2 i) \tan \phi}{rz \cos i \times \sin i} = \frac{\cos i \tan \phi}{\sin i} \Rightarrow \frac{\tan \phi}{\frac{\sin i}{\cos i}}$$

$$\Rightarrow \boxed{FOS = \frac{\tan \phi}{\tan i}}$$

Note: i) FOS > 1 Then soil is in safe condition

ii) FOS < 1 Then soil is in un-safe condition

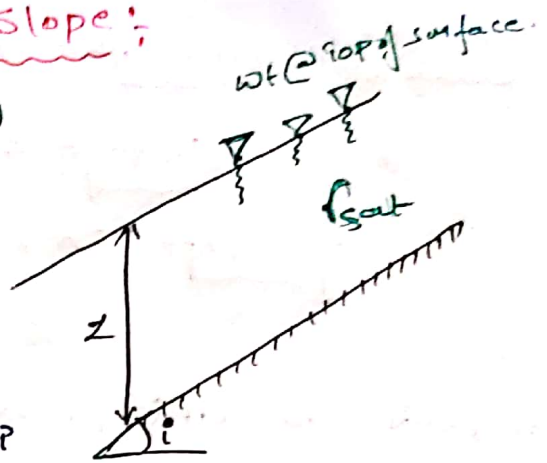
⇒ To satisfy FOS > 1 Then $i < \phi$ {for cohesion less soil's only} such that soil is in safe condition

Fully Submerged - Infinite Slope:

Case (ii) (Cohesion less soil i.e. $c=0$)

w.k.t $\sigma_n' = \sigma_v' \cos i$

in Submerged condition $\left\{ \begin{array}{l} v = \gamma_{sub} \cdot z \\ \sigma_n = \sigma_n' \end{array} \right.$
 So $\sigma_n' = \gamma_{sub} \cdot z \cdot \cos^2 i$ Bcz of p.w.p



Like wise w.k.t

$$\tau = \sigma_v' \sin i$$

$$\tau = \gamma_{sub} z \cdot \cos^2 i \times \sin i$$

So $f.o.s = \frac{\tau_t}{\tau} = \frac{\cancel{\gamma_{sub}} z \cos^2 i \tan \phi'}{\cancel{\gamma_{sub}} z \cos^2 i \sin i}$

ϕ' = Effective angle of internal friction

ϕ = Total angle of internal friction.

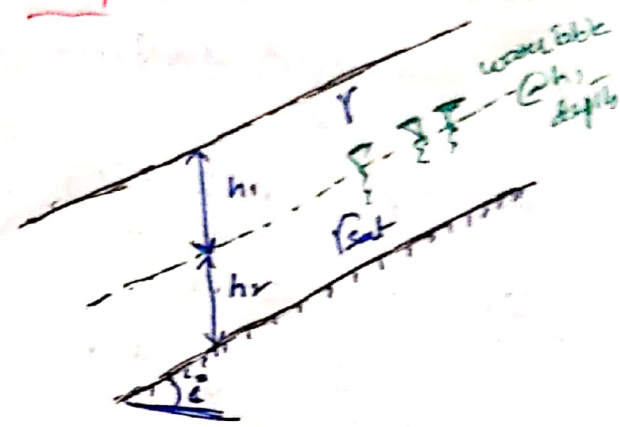
$$f.o.s = \frac{\gamma_{sub} z \cos^2 i \tan \phi'}{\gamma_{sub} z \cos^2 i \sin i} \Rightarrow \frac{\cos^2 i \tan \phi'}{\sin i}$$

on re-arranging

we get $f.o.s = \frac{\tan \phi'}{\left(\frac{\sin i}{\cos i} \right)} \Rightarrow f.o.s = \frac{\tan \phi'}{\tan i}$

NOTE:- To increase the f.o.s we should keep less i value than the ϕ' value.

Case-(iii) Water Table at any depth in cohesionless soil
and Seepage occurs parallel to the Surface
of slope in infinite slope:



=> In this case w.t is presenting @ a depth of h_1 from surface.

=> So the soil which presenting above w.t is may be dry soil or may be partially saturated.

=> In case of dry soil $\gamma = \gamma_d$ &
 for partially saturated soil $\gamma = \gamma_{bulk}$.

Here we assuming dry soil i.e γ .

So w.k.T $\sigma'_n = \sigma'_v \times \cos i$ Here σ'_v is Effective stress

$$\sigma'_n = (\gamma h_1 + \gamma_{sat} h_2 - \gamma_w h_2) \cos i \times \cos i$$

w.k.T { Effective stress = Total stress - p.w.p }

$$\sigma'_n = [\gamma h_1 + h_2 (\gamma_{sat} - \gamma_w)] \cos^2 i$$

w.k.T $\sigma'_v = \gamma z \times \cos i$

$\gamma_w =$ unit wt of water

$$\sigma'_n = [\gamma h_1 + h_2 \times \gamma_{sub}] \cos^2 i$$

w.k.T $\gamma_{sat} - \gamma_w = \gamma_{sub}$

$$\tau = \sigma'_n \times \sin i$$

$$\tau = [\gamma h_1 + \gamma_{sub} h_2] \cos i \cdot \sin i$$

(=> In calculation of τ we are not considering p.w.p Bcz The pressure due to seepage & p.w.p cancels each other Bcz they both are in same direction)

$$FOS = \frac{\tau_f}{\tau} = \frac{\sigma'_n \tan \phi'}{\tau}$$

$$FOS = \frac{(\gamma h_1 + \gamma_{sub} h_2) \cos^2 i \tan \phi'}{(\gamma h_1 + \gamma_{sub} h_2) \cos i \times \sin i}$$

$$FOS = \left(\frac{\gamma_{hi} + \gamma_{sub} h_2}{\gamma_{hi} + \gamma_{sat} h_2} \right) \frac{\tan \phi'}{\tan i}$$

Note: water reaches to the top surface & if seepage occurs.

i.e. $h_1 = 0$ & total height = h_2

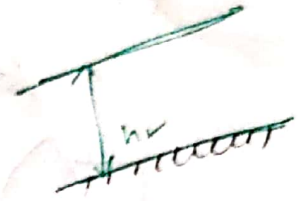
Substitute these values in above eqn

we get

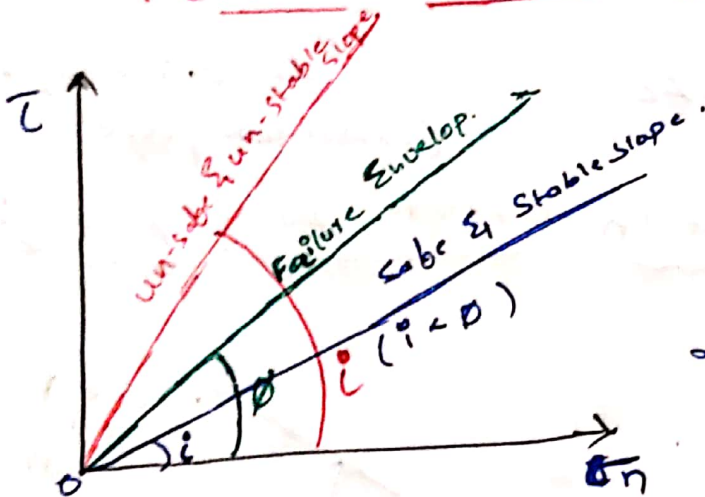
$$FOS = \frac{\gamma_{sub} \times \tan \phi'}{\gamma_{sat} \tan i}$$

$$FOS \approx \frac{1}{2} \times \frac{\tan \phi'}{\tan i}$$

In this case minimum FOS should be > 2 .



∴ Infinite slope in cohesionless soil!



⇒ when if $c=0$, then failure envelope starts from origin (0)

⇒ failure envelope shows the state of strength.

⇒ Mohr's circle below failure envelope shows the state of stress.

⇒ if Mohr's circle is below failure envelope then soil is safe

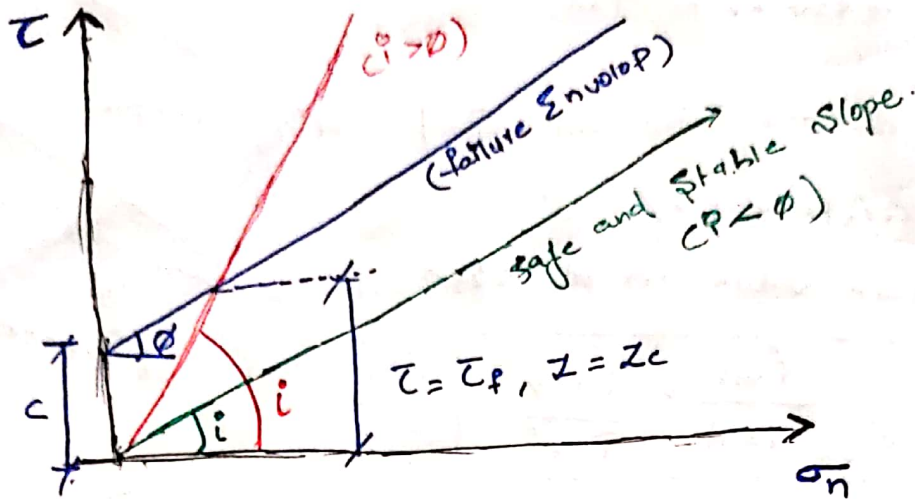
⇒ if Mohr's circle touches or exceeds (i.e. stress $>$ strength) then soil fails.

Note: In case of cohesionless soil's in infinite slope angle of slope (i)

should be less than angle of

internal friction (or) angle of shearing resistance (ϕ).

Infinite Slope in Cohesive Soil [c-φ soil]:



Note:- In case of cohesive soil in Infinite Slope.

⇒ if $i < \phi$ then it is safe and stable but

⇒ if $i > \phi$ then also it can be safe and stable

if $\tau < \tau_f, z < z_c$

z_c : critical depth
(i.e. max depth of slope).

Case (ii). Infinite Slope in Cohesive Soil [c-φ soil]:

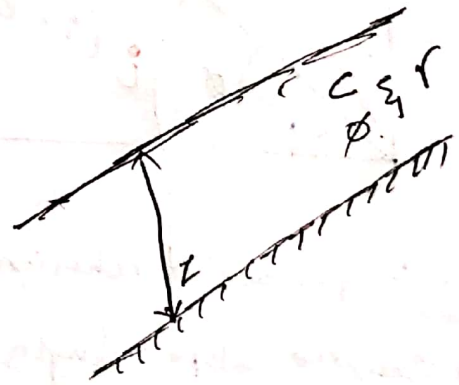
$$FOS = \frac{\tau_f}{\tau} = \frac{c + \sigma_n \tan \phi}{\tau}$$

$$FOS = \frac{c + \gamma z \cos^2 i \tan \phi}{\gamma z \cos i \tan i} \rightarrow (1)$$

$$FOS = \frac{c}{\gamma z \cos i \tan i} + \frac{\gamma z \cos^2 i \tan \phi}{\gamma z \cos i \tan i}$$

$$FOS = \frac{c}{\gamma z \cos i \cdot \tan i} + \frac{\tan \phi}{\tan i} \rightarrow (2)$$

Compare this eqn with case-(i) In this case FOS is ↑ due to cohesion - so we can keep ($i > \phi$)



For critical condition, $Fos = 1$.

If $Fos = 1$, Then $Z = Z_c$, $\tau_f = \tau$

Substitute above values in Eqn (1). we get-

$$1 = \frac{c + f Z_c \cos^2 i \tan \phi}{f Z_c \cos i \sin i}$$

$$f Z_c \cos i \sin i = c + f Z_c \cos^2 i \tan \phi$$

$$c = f Z_c \cos i \sin i - f Z_c \cos^2 i \tan \phi$$

$$c = f Z_c \cos^2 i \left[\frac{\sin i}{\cos i} - \tan \phi \right]$$

$$\frac{c}{f Z_c} = \left[\tan i - \tan \phi \right] \cos^2 i = S_n.$$

$S_n =$ Taylor's
Stability
Number.

So

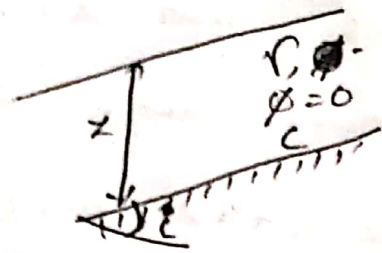
$S_n = \left[\tan i - \tan \phi \right] \cos^2 i$
$S_n = \frac{c}{f Z_c}$

Infinite Slope in clay soil ($\phi=0$)

$$FOS = \frac{\tau_f}{\tau} = \frac{c + \sigma_n \tan \theta}{\tau}$$

but $\phi=0$. So

$$FOS = \frac{c}{\tau} \quad [\because \tan \theta = 0]$$



$$FOS = \frac{c}{r z \cos i \sin i}$$

for critical condition w.k.t $FOS=1$, $z=z_c$.

$$\text{So } 1 = \frac{c}{r z_c \cos i \sin i}$$

$$\cos i \cdot \sin i = \frac{c}{r z_c}$$

w.k.t $\frac{c}{r z_c} = S_n$ i.e Taylor's Stability Number

$$\text{So } S_n = \cos i \times \sin i$$

Short cut to remember above formula:

$$\text{w.k.t for } c-\phi \text{ soil } S_n = (\tan i - \tan \theta) \cos^2 i$$

put $\phi=0$ in above eqn

$$S_n = (\tan i - \tan 0) \cos^2 i$$

$$S_n = \tan i \times \cos^2 i$$

$$S_n = \frac{\sin i}{\cos i} \times \cos^2 i$$

$$S_n = \sin i \times \cos i \quad \rightarrow \text{for clay soil}$$

Stability Analysis by Swedish Arc Method;

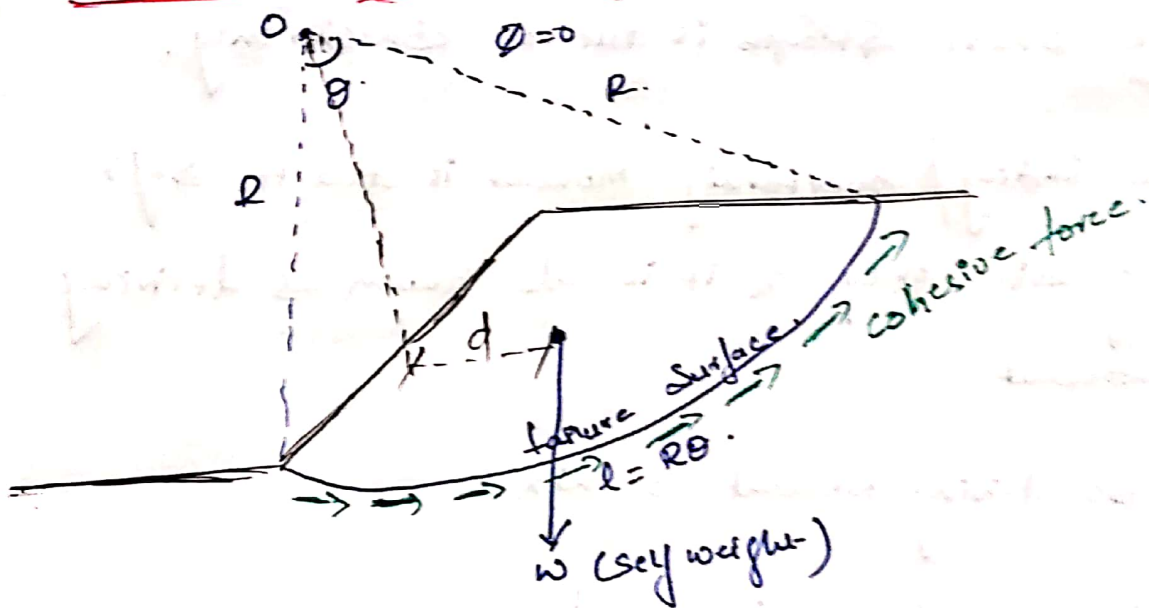
⇒ this method is used to study the analysis of finite slopes.

Finite slope:- If the slope is of finite dimension & bounded by top & bottom surface is termed as finite slope.

⇒ In finite slopes failures occur due to rotation, & failure surfaces are may be circular or spiral.

⇒ This method is applicable for c & $c-\phi$ soils.

(i) Check for stability of c -soil:-



⇒ let us take a finite slope which is having a slip failure surface.

⇒ Consider the moments about 'O' which is having radius 'R' & making an angle θ with failure surface.

⇒ here 'W' is self wt of soil which acts vertically downwards

⇒ here length of Arc i.e failure surface is 'l'.

$$l = R \cdot \theta$$

⇒ here soil slides due to self wt 'w'.

⇒ cohesive forces which are developed in soil will resist

The sliding moment of soil.

⇒ So cohesive forces are formed due to shear

Strength of soil's.

w.k.t Shear Strength $\tau_s = c + \sigma \tan \phi$

here $\phi = 0$ so

$$\tau_s = c.$$

i.e Shear strength is due to cohesion only.

⇒ here sliding/overturning moment is due to self wt of soil only & it is also known as driving moment.

⇒ So driving moment = $w \times d$.

Resisting moment = force \times lever arm.

$$\text{Arc length } (l) = R \cdot \theta$$

$$\text{Resisting force} = c \times \text{area of plane}$$

$$= c \times R \theta \times 1$$

$$= c \times R \theta$$

$$\text{Resisting moment} = c R \theta \times R$$

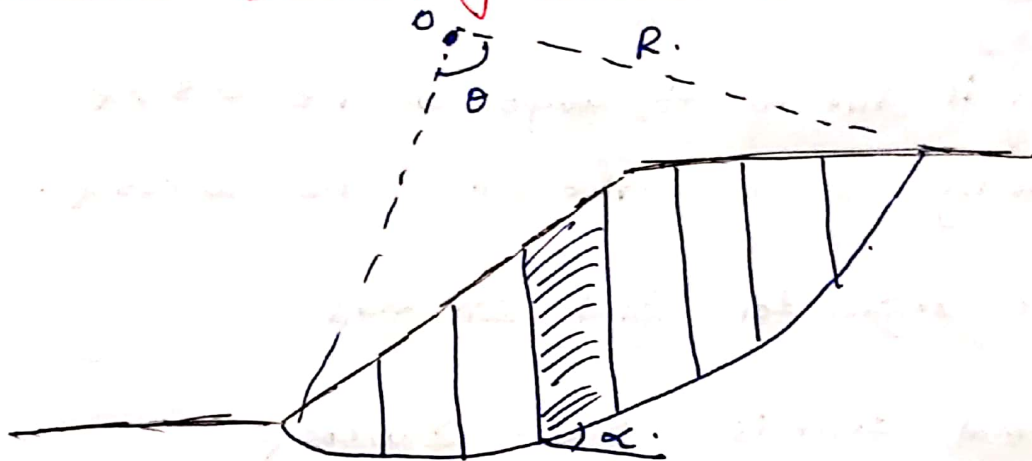
$$= c R^2 \theta$$

$$Fos = \frac{\text{Resisting moment}}{\text{driving moment}} = \frac{cR^2\theta}{wxd}$$

$$Fos = \frac{cR^2\theta}{wxd}$$

- if $Fos > 1$ slope is safe.
- $Fos < 1$ slope fails/un-safe.
- $Fos = 1$ critical condition.

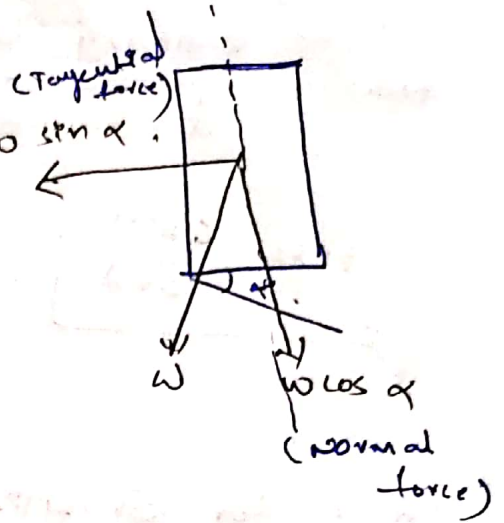
Check for Stability of c- ϕ Soil:



- \Rightarrow In this method c- ϕ soil is assumed to be divided into no. of slices of equal width having unit thickness.
- \Rightarrow No. of slices should be > 5 (or) $(6-12)$.
- \Rightarrow Each slice of soil mass acts like independent column & it is assumed that there is no forces b/w adjacent slices.
- \Rightarrow slice is making an angle ' α ' with horizontal.

Consider a Single Slice.

⇒ say wt 'w' acting vertically downwards



∴ w is having two Components.

Vertical ∴ horizontal.

h_z component = $w \sin \alpha$

Vertical " = $w \cos \alpha$.

⇒ Sliding is due to h_z component i.e $w \sin \alpha$.

⇒ Resisting " " " vertical " " i.e $w \cos \alpha$.

⇒ if we consider for Total soil mass

Normal force is $\Sigma N = \Sigma w \cos \alpha$

Tangential force $\Sigma T = \Sigma w \sin \alpha$.

⇒ here driving moment is due to tangential forces.

⇒ force x lever arm.

driving moment ⇒ $\Sigma T \sin \alpha \times R$.

⇒ Resisting moment is due to Shear Strength.

⇒ Shear Strength is due to c & ϕ .

we k.T c value from previous sum

$$c = c R^2 \theta$$

Resisting moment due to friction is

~~at a time~~

σ is normal stresses so

$$\sigma = (\Sigma NT \tan \alpha) R.$$

Resisting moment = $CR^2 \theta + \Sigma NT \tan \alpha R.$

So FOS =
$$\frac{CR^2 \theta + \Sigma NT \tan \alpha R}{\Sigma T \times R.}$$

$$FOS = \frac{CR\theta + \Sigma W \cos \alpha \tan \alpha}{\Sigma W \sin \alpha}$$

FOS < 1 unsafe.

FOS > 1 safe.

FOS = 1 Critical Condition.

Factor of safety with different components of soil.

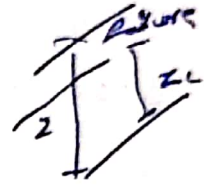
⇒ FOS of cohesive soil can be represented in terms of height also.

1) F.O.S of cohesive soil in terms of height

$$FOS(H) = \frac{H_c}{H} \text{ or } \frac{Z_c}{Z}$$

H_c : Critical height of slope

H : Total height of slope.



2) FOS in terms of cohesion.

i) $H < H_c$ (or) $Z < Z_c$

$$(FOS)_c = \frac{C}{C_m}$$

C : Total cohesion

C_m : Mobilised (utilised) cohesion

w.r.t $S_n = \frac{C}{\sqrt{1} \times Z_c}$

③ F.O.S with friction [Angle of internal friction]

⇒ It is the ratio of available frictional strength to the mobilised frictional strength

$$(FOS)_\phi = \frac{\sigma_n \tan \phi}{\sigma_n \tan \phi_m}$$

$$FOS_\phi = \frac{\tan \phi}{\tan \phi_m}$$

Min $S_n = 0.261$

Taylor's Stability Number method:

⇒ In this method stability of slope is analysed with the help of Taylor's Stability Number which is taken from Taylor's chart on the basis of given c & ϕ values.

w.k.t from previous derivations,

Taylor's Stability No. (S_n)

$$S_n = \frac{c}{\gamma \times H_c} \text{ or } \frac{c}{\gamma \times Z_c}$$

we can modify the S_n into various forms.

i.e. $S_n = \frac{c}{\gamma \times Z_c}$

w.k.t $f = \frac{Z_c}{Z}$

so $Z_c = f \times Z$

$$S_n = \frac{c}{\gamma \times f \times Z} \text{ in terms of } F.O.S$$

w.k.t $\Rightarrow F = \frac{c}{C_m}$

w.k.t $\frac{c}{F} = C_m$ if we keep it in above S_n

$$C_m = \frac{c}{F}$$

$$S_n = \frac{C_m}{\gamma \times Z}$$

here S_n is in terms of mobilised cohesion.

$$f = \frac{c}{\gamma S_n H}$$

Culmann's Graphical method for Estimating

Active Earth Pressure

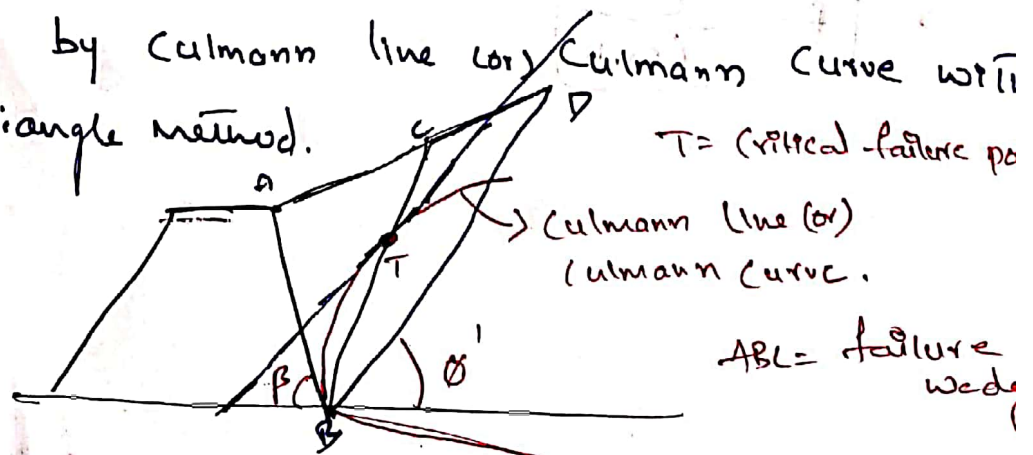
⇒ In 1866 Culmann's given Earth Pressure Theory graphically to Estimate Active Earth pressure.

⇒ it was depending on Coloumb's Earth pressure theory i.e. Coloumb's wedge theory.

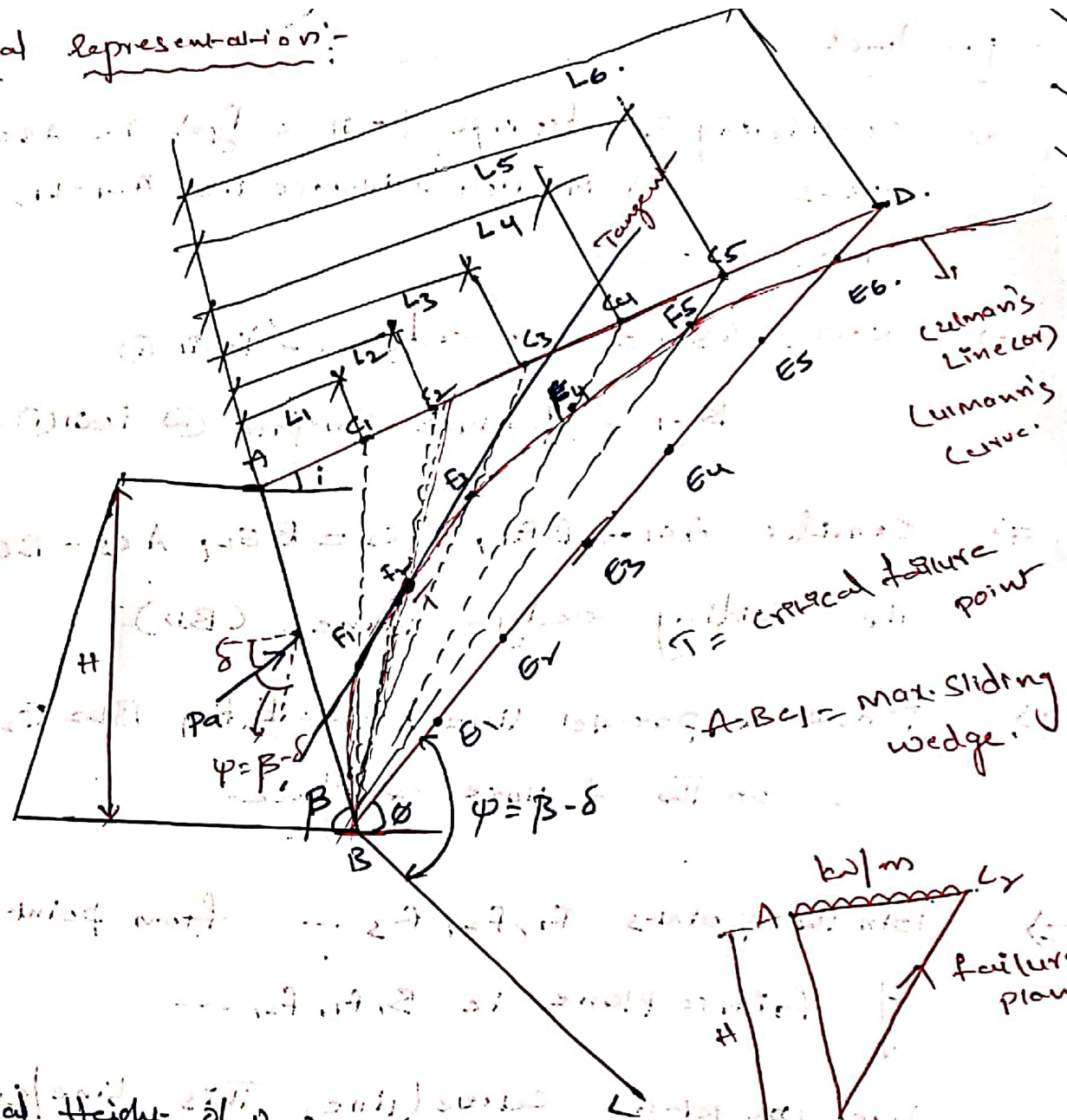
⇒ In this theory the failure wedge is experiencing diff. type's of "Surcharge load's" [e.g. UDL (kN/m^2), Line load (k)] whereas in "distb wedge theories" only a single type of load is taken in to account.

⇒ due to various type's of surcharge load's on failure wedge there will be a "critical failure plane" is formed, along with the Culmann's line. (or) Culmann Curve.

⇒ So Culmann's considered to determine the active Earth Pressure by Culmann line (or) Culmann Curve with force triangle method.



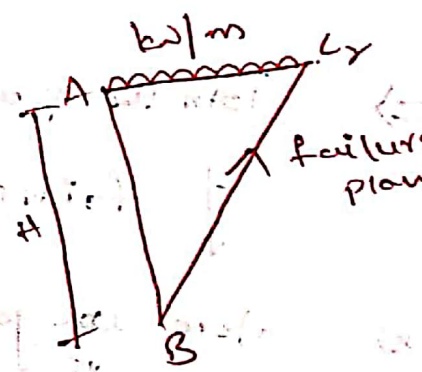
graphical representation:-



Culman's Line (or) Lurmann's Curve.

T = critical failure point

A-B-C1 = max. sliding wedge.



H = vertical height of R.W.

i = slope angle of back fill

beta = angle of failure plane

Procedure:

- \Rightarrow Considering the triangle trail wedges i.e. $ABC_1, ABC_2, ABC_3, \dots$ & mention distance i.e. $AC_1 = L_1, AC_2 = L_2, AC_3 = L_3, \dots$
- \Rightarrow Now, $ABC_1 =$ wt of wedge @ Trail ①
 $BC_1 =$ failure surface @ Trail ①.
- \Rightarrow Consider $AC_1 = BE_1, AC_2 = BE_2, AC_3 = BE_3, \dots$
The sliding wedge plane, (BD).
- \Rightarrow Draw a parallel line, $BL = E_1F_1, BL = E_2F_2, BL = E_3F_3, \dots$
... on the failure surface.
- \Rightarrow Join the points F_1, F_2, F_3, \dots from point B to end of failure plane, i.e. B, F_1, F_2, \dots
- \Rightarrow Here we get a curve/line. This line/curve we call as Culmann's line / Culmann's curve.
- \Rightarrow Draw a tangent line to Culmann's curve. This tangent should be parallel to sliding/failure plane.
- \Rightarrow Tangent intersecting point on curve is taken as failure point.

Module - III

③ Explain briefly various types of shear failures in shallow foundations. Mention the parameters to decide type of shear failure?

Ans: There are three methods that shallow foundation failure occurs.

a) General Shear failure

b) Local shear failure

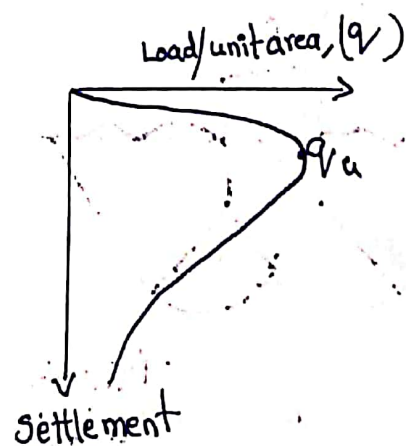
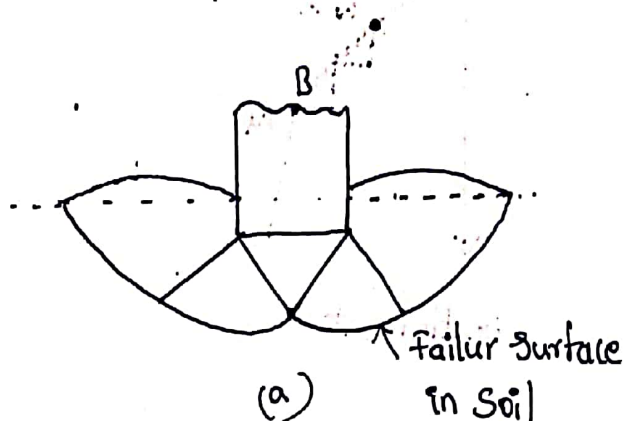
c) Punching shear failure

a) General Shear Failure:

A gradual increase in the load on the foundation will increase the settlement of the footing and rises the pressure under the foundation.

When the pressure under the foundation reaches the ultimate pressure that the soil can bear, the foundation will fail suddenly.

These types of foundation failures occurs in low compressible soils.



The ultimate pressure that soil can bear is the Ultimate bearing Capacity of the foundation. As indicated in the above, when the load reaches the ultimate bearing capacity (P_{hu}), it fails

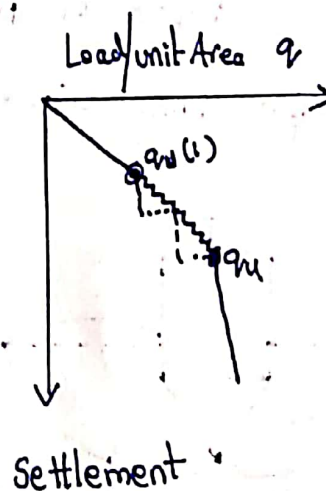
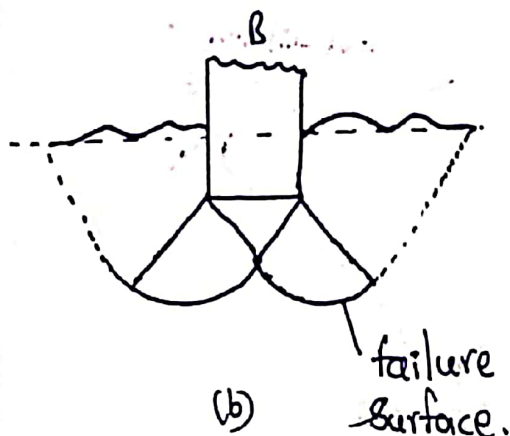
- 1) This type of shallow foundation failure occurs in dense sand, (or) stiff cohesive soil.
- 2) Dense and stiff soils are low compressible leads to shear failure.
- 3) Tilting of foundation occurs when fail.

Local Shear failure:-

Local shear failure occurs in medium compressible soil.

An increase in the pressure in the foundation increases the settlement of the foundation and the failure surface in the soil gradually extends outwards from the foundation.

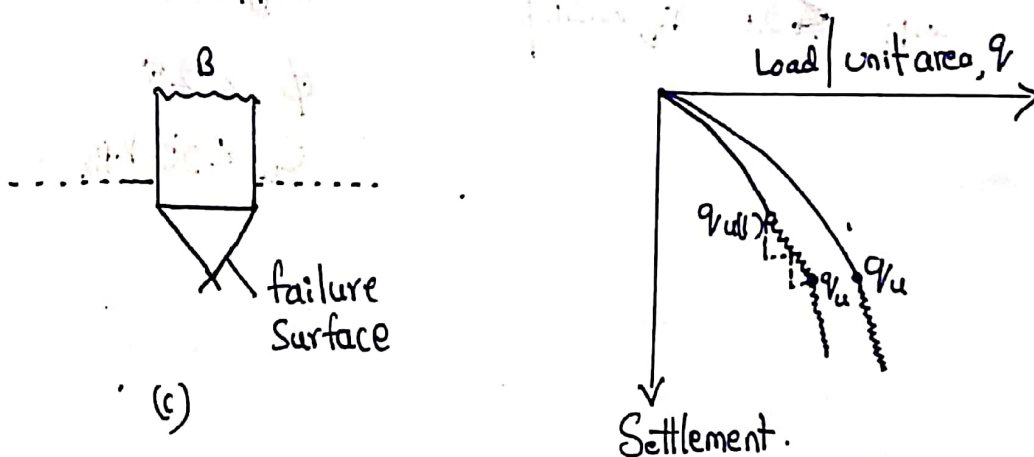
Failure surface does not extend to the ground surface as the soil is compressible (or) due to the deeper depth of the foundation.



Punching Shear failure:- This type of failure occurs when the foundation is rested on fairly loose soil where the settlement of the foundation is higher.

Shear surfaces are not developed due to the compressibility of soil.

The soil under the foundation compressed and it cannot bear the pressure applied from the foundation.



The above figure indicates the failure surface and the load settlement curve of the foundation.

The parameters to decide type of shear failure.

General shear failure:- This failure is accompanied by low strain ($< 5\%$) in a soil considerable ϕ ($\phi > 36^\circ$) and large "N" ($N > 30$) and high relative density I_D ($I_D > 70$)

i.e strain $< 5\%$

$I_D > 70$

$N > 30$

$\phi > 36^\circ$

$C_u > 100 \text{ kPa}$

Local/Punching Shear Failure

large strain (> 10 to 20%) in a soil with considerably low ϕ ($\phi < 28^\circ$) and low N ($N < 5$) having low relative density I_D ($I_D < 20\%$)

i.e. large strain $\rightarrow 20\%$

$N > 5$

$I_D < 20, I_D < 20$

i.e. strain $> 20\%$

$N < 5$

$I_D < 20$

$\phi < 28^\circ$

$C_u < 50 \text{ kPa}$

④ Explain with neat sketch, various types of shallow foundation? ⑤

Ans:- Shallow Foundation :- Foundation is placed immediately lowest part of the Super structure, is termed as Shallow Foundation.

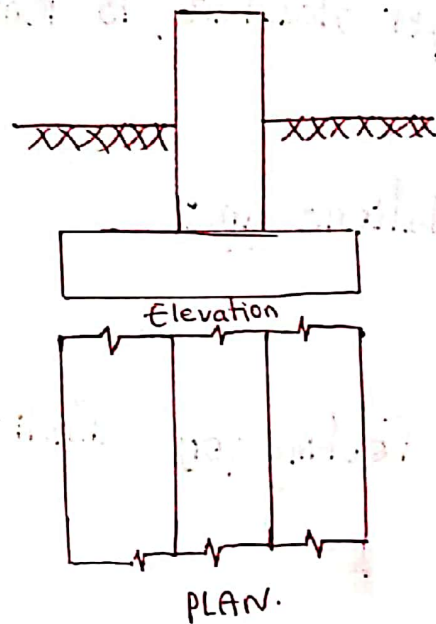
Types of Shallow Foundations are:

- 1) Strip Footing
- 2) Spread or Isolated Footing (or) Individual Footing
- 3) Combined footing
- 4) Strap (or) Cantilever Footing
- 5) Mat (or) Raft Foundations.

① Strip Footing :-

- a) A strip footing is provided for a load-bearing wall
- b) A strip footing is also provided for a row of columns which are so closely spaced that their spread footings overlap or nearly touch each other.
- c) In such a case, it is more economical to provide a strip footing than to provide a number of spread footings in one line.
- d) A strip footing is also known as Continuous footing.
- e) Strip footing also prevent the horizontal distortion of individual foundation and strengthen them.

f) In the horizontal direction, the strip footings act as a continuous carrier under the force influence from the columns/walls.



3) Spread (or) Isolated Footing (or) Individual Footing

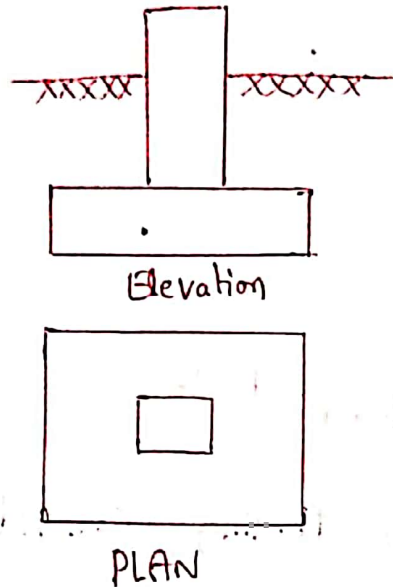
a) A Spread footing also called as isolated footing, Pad footing and individual footing is provided to support an individual column.

b) A spread footing is circular, square (or) rectangular slab of uniform thickness.

c) Sometimes, it is stepped (or) haunched to spread the load over a large area.

d) Nowadays, massive foundations are avoided and reinforced spread footing are performed with considerably smaller dimensions due to the use of reinforcement.

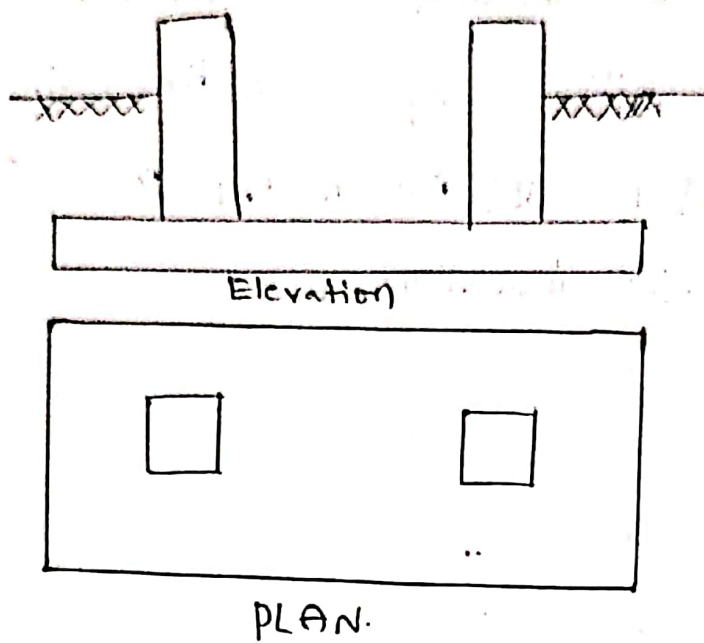
e) The criterion for the foundation determination of spread foundation stiffness depends on the soil foundation reactor module and is valid for $k > 0.40$ for solid foundation i.e. $k < 0.40$ for flexible foundations.



Spread Footing

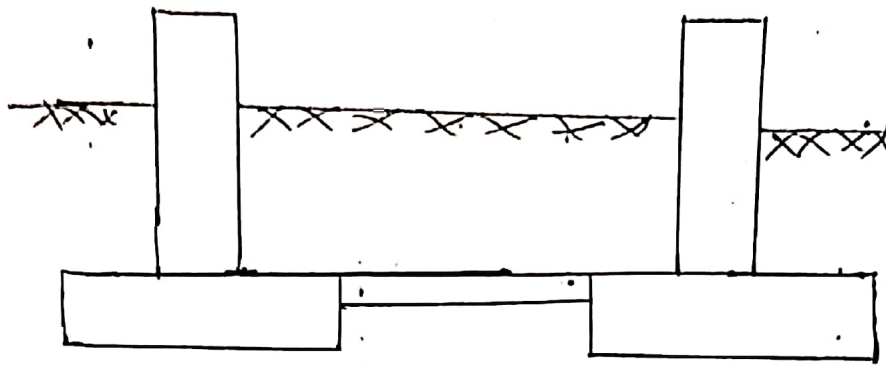
③ Combined Footing:

- a) A Combined Footing supports two columns.
- b) It is used when the two columns are so close to each other that their individual footings would overlap.
- c) A combined footing is also provided when the property line is so close to one column that a spread footing would be eccentrically loaded when kept entirely within the property line.
- d) By combining it with that of an interior column, the load is evenly distributed.
- e) A Combined footing may be rectangular (or) trapezoidal in plan.

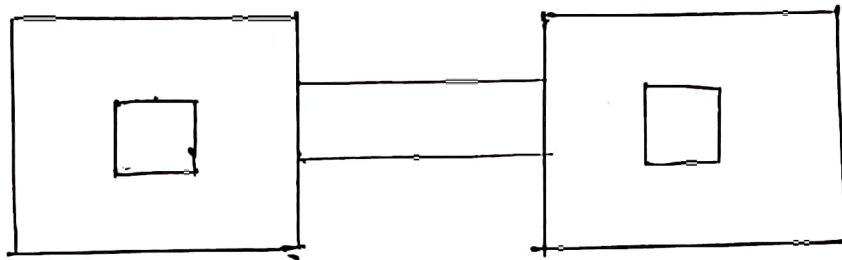


4) Strap (or) Cantilever Footing

- a) A Strap (Cantilever) Footing consist of two isolated footing connected with a structural strap (or) lever.
- b) The Strap connects the two Footings such that they behave as one unit.
- c) The strap is designed as a rigid beam
- d) The individual footings are so designed that their combined line of action passes through the resultant of the total load.
- e) a strap footing is more economical than a Combined Footing when the allowable soil pressure is relatively high and the distance between the columns is large.



ELEVATION



PLAN

Strap (or) Cantilever footing

5) Mat (or) Raft Foundation

a) A mat (or) Raft foundation is a large slab supporting a number of columns and walls under the entire structure (or) a large part of the structure.


b) A mat is required when the allowable soil pressure is low (or) where the columns and walls are so close that individual Footings would overlap (or) nearly touch each other

c) Mat foundations are useful in reducing differential settlements on non-homogeneous soils (or) where there is

Terzaghi's Bearing Capacity Theory

- => In 1943 Terzaghi's given a Theory to determine the bearing capacity of soil which is extended from Prandtl (1920) Eqn.
- => Terzaghi made following assumption's for developing bearing capacity Eqn to determine ultimate bearing capacity (q_u) for $c-\phi$ soil.

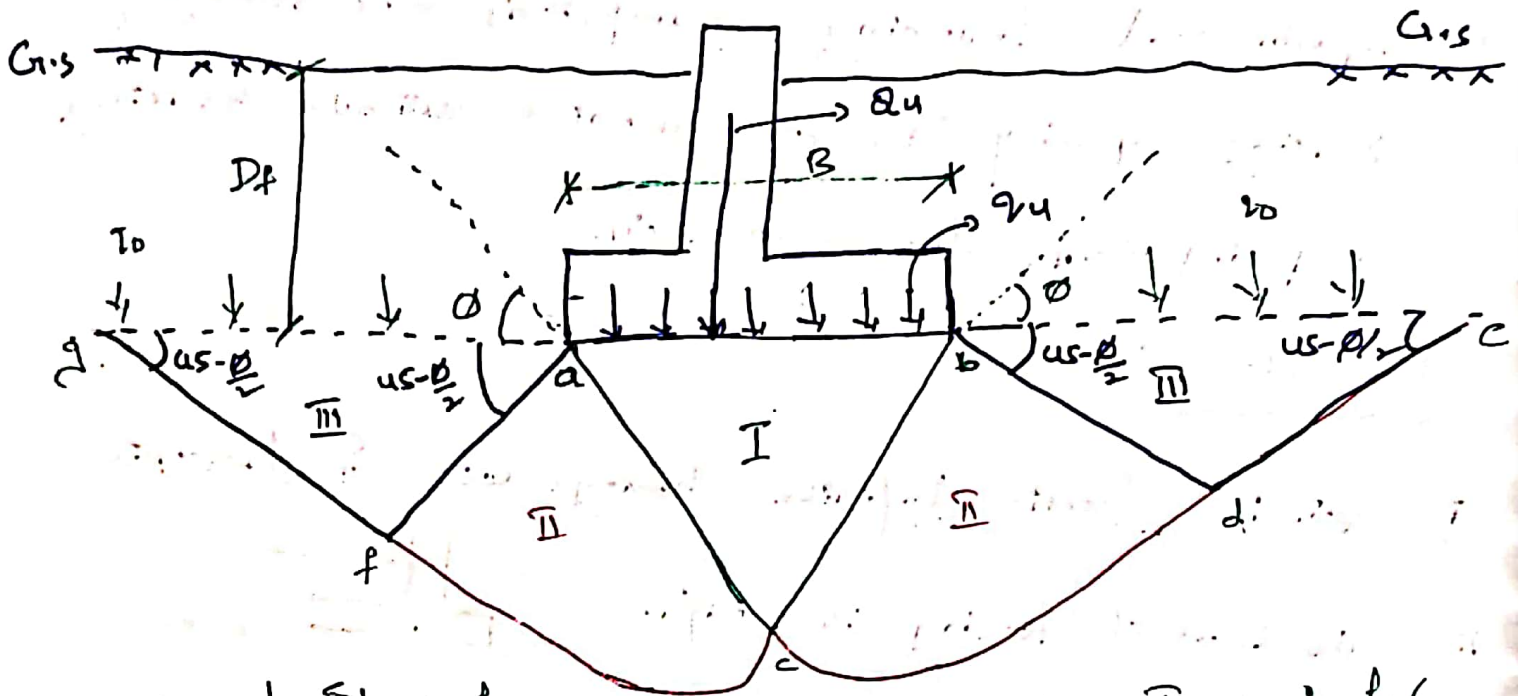
Assumption's:

- i) Soil is Semi-Infinite, homogeneous & isotropic.
- ii) The Base of footing is rough. 
- iii) Foundation is shallow type i.e. ($\frac{D_f}{B} < 1$).
- iv) footing is continuous / strip footing i.e. ($L \gg B$) & it makes analysis 2-dimensional along the depth & width.
- v) Soil will fail's when it reaches to plastic equilibrium.
- vi) The load is vertical & symmetrical.
- vii) The ground surface is horizontal along with foundation.
- viii) The failure is only by general shear failure.
- ix) The stress zone acts only @ Base of footing.
- x) The over burden pressure @ foundation level is equivalent to surcharge load i.e. ($\sigma_0 = \gamma \cdot D_f$)
(Here γ = U.W of soil, D_f = Depth of foundation)

xi) The principle of Superposition is valid

xii) Coulomb's law is strictly valid, i.e. $(\sigma = c + \sigma \tan \phi)$

Failure Mechanisms:



General Shear failure surface as assumed by Terzaghi for strip footing.

Zone I = Elastic Equilibrium State.

Zone II = Radial Shear State.

Zone III = Rankine's passive State.

Here q_u = load per unit area

B = width of footing.

Ultimate bearing capacity S_u :-

$$q_u = c N_c + \gamma D_f N_1 + \frac{1}{2} \cdot \gamma \cdot B \cdot N_2$$

$$q_u = c N_c + \gamma N_1 + \frac{1}{2} \gamma B N_2$$

Here B = width of footing

D_f = Depth of footing below G.L.

$\gamma \cdot D_f$ = Surcharge load @ foundation level

$N_c, N_1, \& N_2$ = Bearing capacity factors
[depend on frictional angle of soil]

$$N_1 = \tan^2 \left(45 - \frac{\phi}{2} \right)$$

$$N_2 = N_1 e^{\pi \tan \phi}$$

$$N_3 = 1.8 \tan \phi (N_2 - 1)$$

$$N_c = \cot \phi (N_2 - 1)$$

For purely cohesive soil = $\left\{ \begin{array}{l} \phi = 0^\circ \\ N_1 = 1 \\ N_2 = 1 \\ N_3 = 0 \end{array} \right.$

If the soil is failure in local shear failure then

Mobilized parameter's are

$$c_m = \frac{2}{3} c, \quad \phi_m = \tan^{-1} \left(\frac{2}{3} \phi \right)$$

Bearing capacities for Dibb soils & footings:-

(i) cohesive soil - strip footing:-

$$\phi = 0, \quad c > 0, \quad N_c = 5.7, \quad N_1 = 0, \quad N_2 = 1$$

$$q_u = c N_c + \gamma D_f N_1 + 0.5 \gamma \cdot B \cdot N_2$$

$$= 5.7 N_c + \gamma D_f N_1 + 0$$

$$q_u = 5.7 N_c + \gamma D_f$$

ii) Non-cohesive soil - Strip footing:

$$q_u = c N_c + (D_f N_q + \frac{1}{2} B \gamma N_\gamma)$$

here $c = 0$, & $\beta = 0$

$$q_u = (D_f N_q + \frac{1}{2} B \gamma N_\gamma)$$

iii) cohesive soil - square footing:

$$q_u = 1.3 c N_c + (D_f N_q + 0.4 B \gamma N_\gamma)$$

iv) Non-cohesive soil - Square footing:

$$q_u = (D_f N_q + 0.4 B \gamma N_\gamma)$$

v) cohesive soil - ~~strip~~ Rectangular footing:

$$q_u = \left[1 + 0.3 \frac{B}{L} \right] c N_c + (D_f N_q + \left[1 - 0.2 \frac{B}{L} \right] \frac{1}{2} B \gamma N_\gamma)$$

vi) Non-cohesive soil - Rectangular footing:

$$q_u = (D_f N_q + \left[1 - 0.2 \frac{B}{L} \right] \times \frac{1}{2} B \gamma N_\gamma)$$

vii) cohesive soil - circular footing:

$$q_u = 1.3 c N_c + (D_f N_q + 0.3 B \gamma N_\gamma)$$

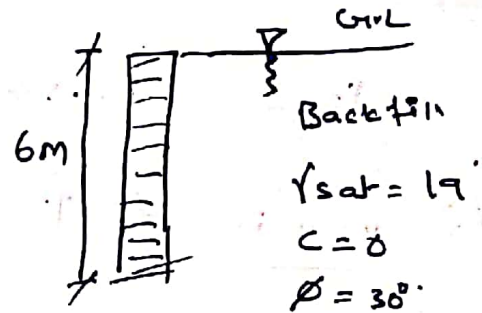
viii) Non-cohesive soil - circular footing:

$$q_u = (D_f N_q + 0.3 B \gamma N_\gamma)$$

Module-2 Q-7.

- ⊕ A masonry P.W with vertical back has to retain a backfill of 6m ht. behind it. The G.L is horizontal @ top & with the w.T is up to top of Backfill, assume $\gamma_{sat} = 19 \text{ kN/m}^3$, $c=0$, $\phi=30^\circ$
- Solve horizontal earth pressures
- wall moves away from Backfill
 - wall moves towards backfill
 - wall is rigid.

Soln:- Given Data:-



(a) wall moves away from Backfill:-

So here active earth pressure is acting. (P_a)

active state $k_a = \frac{1 - \sin \phi}{1 + \sin \phi}$

when Backfill is submerged two types of pressures acts on wall

- active E-P due to submerged wt of soil (P_a)
- Lateral earth pressure due to water. (P_w)

so total pressure $\bar{P}_a = P_a + P_w$

w.k.t $P_a = \frac{1}{2} \gamma_{sat} k_a H^2$, $P_w = \frac{1}{2} \gamma_w H^2$

So $\bar{P}_a \Rightarrow \frac{1}{2} \gamma_{sat} k_a H^2 + \frac{1}{2} \gamma_w H^2$

w.k.t $\gamma_{sat} = 19$, $k_a = \frac{1 - \sin \phi}{1 + \sin \phi} =$, $H = 6$, $\gamma_w = 9.81$
(Taken)

So $\bar{P}_a = (0.5) (19) (0.33) (6)^2 + (0.5) (9.81) (6)^2$

$\bar{P}_a = 289.44 \text{ kN/m}$

② wall moves toward's back fill:-

it is in passive condition.

$$k_p = \frac{1 + \sin \theta}{1 - \sin \theta} = 3.$$

$$\text{So } \bar{P}_p = \frac{1}{2} k_p \cdot (\rho \cdot x \cdot H^2) + \frac{1}{2} \times \rho \times H^2$$

$$\Rightarrow 0.5 \times 3 \times 19 \times 6^2 + 0.5 \times 19 \times 6^2$$

$$\therefore \bar{P}_p = 1202.58 \text{ kN/m}$$

③ wall is rigid:-

① but condition $k_0 = 1 - \sin \theta$

$$k_0 = 1 - \sin 30 = 0.5$$

$$\text{So } P_0 = \frac{1}{2} \times k_0 \times (\rho \cdot x \cdot H^2)$$

$$= 0.5 \times 0.5 \times 19 \times 6^2$$

$$P_0 \Rightarrow 171 \text{ kN/m}$$

module - 2

Q 2: a wall with a smooth vertical back 9 m high supports a purely cohesive soil $c = 20 \text{ kN/m}^3$ & $\gamma = 18 \text{ kN/m}^3$ solve

- i) Maximum depth of Tension crack.
- ii) active force before tensile crack
- iii) active force after Tensile crack occurs.

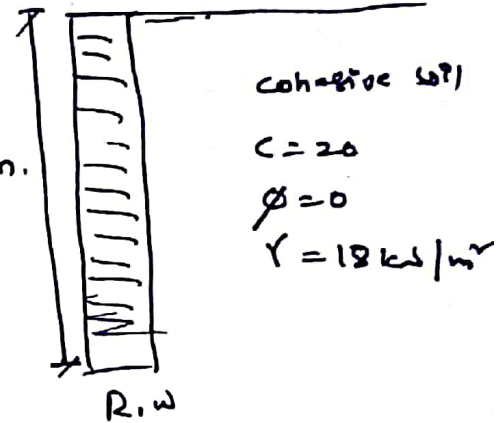
Soln:-

i) Maximum depth of Tension crack:- (z_c) m.

$$z_c = \frac{2c}{\gamma \sqrt{K_a}}$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} \Rightarrow 1$$

$$z_c = \frac{2 \times 20}{18 \times 1} \Rightarrow \frac{40}{18} = 2.22$$



ii) active force before tensile crack:-

w.k.t active force before tensile crack is

$$P_a = \frac{1}{2} \times \gamma \times H^2 - 2cH$$

$$\Rightarrow 0.5 \times 18 \times 9^2 - 2 \times 20 \times 9.$$

$$P_a = 369 \text{ kN/m.}$$

iii) active force after Tensile crack:-

active force after Tensile crack is

$$P_a = \frac{1}{2} (\gamma H - 2c) (H - z_c)$$

$$\Rightarrow 0.5 (18 \times 9 - 2 \times 20) (9 - 2.22)$$

$$P_a = 414.8 \text{ kN/m.}$$